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Infosys vs. Wipro: A Comparative Financial Performance Analysis

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Abstracts:

This study presents a comparative financial performance analysis of Infosys Ltd. and Wipro Ltd., two of the leading information technology service companies in India. The analysis evaluates the financial performance of both companies over a five-year period from FY2021 to FY2025. Key financial indicators such as revenue growth, net profit, operating margin, earnings per share, return on equity (ROE), liquidity ratios, and debt-equity ratio have been examined.

The study aims to assess the financial strength, profitability, operational efficiency, and market performance of both companies. Comparative financial analysis helps investors, researchers, and stakeholders understand the relative strengths and weaknesses of these firms in the competitive Indian IT sector.

The findings reveal that Infosys demonstrated stronger and more consistent financial performance than Wipro during the study period. Infosys showed higher revenue growth, better profitability, superior operational efficiency, and lower financial risk. Although Wipro maintained healthy liquidity and better five-year share price returns, Infosys emerged as the financially stronger organization overall.

Keywords: Financial Analysis, Comparative Study, Infosys Ltd., Wipro Ltd., IT Industry, Revenue Growth, Profitability, Financial Ratios, Operating Margin, Liquidity, Return on Equity, Indian IT Companies.

Introduction:

The Indian Information Technology (IT) industry is one of the major contributors to the country's economic growth and global recognition. Companies such as Infosys Ltd. and

Wipro Ltd. have established themselves as global leaders in IT consulting, outsourcing, cloud computing, and digital transformation services.

Financial performance plays a significant role in determining the competitiveness and sustainability of IT companies. Investors, management, and stakeholders rely on financial analysis to evaluate profitability, operational efficiency, liquidity, and long-term growth potential.

This study focuses on a comparative financial analysis of Infosys and Wipro for the period FY2021–FY2025. The analysis is based on secondary data collected from annual reports, financial websites, and market reports.

Review of Literature:

Several researchers have studied the financial performance of Indian IT companies.

Sharma (2022) concluded that Infosys maintained stronger profitability and operational efficiency compared to its competitors in the Indian IT sector.

Rao and Mehta (2023) observed that digital transformation services significantly improved the revenue growth of major Indian IT firms.

Patel (2024) highlighted that companies with lower debt and stronger liquidity positions were better able to manage market uncertainties in the IT industry.

Previous studies indicate that profitability, operational efficiency, and strategic investments are critical determinants of long-term growth in the IT sector

Research Methodology:

This study is analytical and comparative in nature.

Sources of Data

The study is based entirely on secondary data collected from:

- Annual reports of Infosys and Wipro
- Moneycontrol
- Economic Times

- NASSCOM reports
- Company investor portals
- Financial databases and websites

Period of Study

The financial data covers five financial years from FY2021 to FY2025.

Tools Used for Analysis

The following financial tools and techniques have been used:

- Comparative financial analysis
- Ratio analysis
- Trend analysis
- Profitability analysis
- Liquidity analysis

Data Analysis & Interpretation: (optional)

Financial Data Analysis

Table 1: Financial Data of Infosys and Wipro (FY2021–FY2025)

Year	Infosys Revenue (₹ Crore)	Infosys Net Profit (₹ Crore)	Wipro Revenue (₹ Crore)	Wipro Net Profit (₹ Crore)
2021	100472	19423	61934	10855
2022	121641	22146	79312	12237
2023	146767	24108	90487	11372
2024	153670	26248	89760	11135

Year	Infosys Revenue (₹ Crore)	Infosys Net Profit (₹ Crore)	Wipro Revenue (₹ Crore)	Wipro Net Profit (₹ Crore)
2025	162990	26750	89088	13192

Research Findings:

The financial data indicates that Infosys achieved consistent revenue and profit growth during FY2021–FY2025.

Infosys revenue increased from ₹100,472 crore in FY2021 to ₹162,990 crore in FY2025, while net profit increased from ₹19,423 crore to ₹26,750 crore.

In contrast, Wipro experienced slower revenue growth after FY2023, with a slight decline in FY2024 and FY2025. However, Wipro's net profit improved moderately in FY2025.

The analysis suggests that Infosys maintained stronger operational efficiency and financial stability throughout the study period.

Ratio Analysis

Table 2: Extended Ratio Analysis (FY2025)

Financial Metric	Infosys	Wipro
ROE (%)	27.87	15.94
Net Profit Margin (%)	16.41	14.80
Debt to Equity Ratio	0.00	0.20
Operating Margin (%)	21.00	17.50
Current Ratio	2.20	2.00

Interpretation of Ratios

1. Return on Equity (ROE)

Infosys reported an ROE of 27.87%, significantly higher than Wipro's 15.94%. This indicates that Infosys utilized shareholders' funds more efficiently.

2. Net Profit Margin

Infosys maintained a stronger net profit margin of 16.41% compared to Wipro's 14.80%, reflecting better cost control and operational management.

3. Debt-Equity Ratio

Infosys operated with negligible debt, indicating lower financial risk and stronger financial stability. Wipro maintained a moderate debt-equity ratio of 0.20.

4. Operating Margin

Infosys demonstrated superior operating efficiency with an operating margin of 21.00%, compared to Wipro's 17.50%.

5. Liquidity Position

Both companies maintained healthy liquidity positions with current ratios above 2.0, indicating their ability to meet short-term obligations.

Analytical Discussion

Trend Analysis

Infosys demonstrated consistent growth in both revenue and profitability due to expansion in digital services, cloud computing, and operational efficiency.

Wipro showed slower growth during the same period. Although profitability remained stable, the company experienced stagnation in revenue growth after FY2023.

Competitive Advantage

Infosys holds a stronger competitive position because of:

- Higher profitability
- Better operational efficiency
- Stronger return on equity
- Lower financial risk
- Diversified global client base

Wipro remains competitive but faces challenges in achieving growth comparable to Infosys.

Risk Assessment

Both companies are exposed to risks such as:

- Currency fluctuations
- Global economic uncertainty
- Geopolitical tensions
- Competition in digital transformation services

However, Infosys possesses stronger balance-sheet stability, reducing its overall financial risk.

Strategic Insights

Infosys appears to be more growth-oriented and financially resilient. Wipro may need additional investments in innovation, acquisitions, and digital transformation services to improve its competitive position.

Additional Comparison: Liquidity and Share Price Performance

Table 3: Liquidity and Share Price Performance

Metric	Infosys	Wipro
Current Ratio (FY2025)	2.2	2.4
Five-Year Share Price Return (%)	53.64	61.91

Analytical Discussion

Liquidity Analysis

Both companies maintain strong liquidity positions. Wipro's current ratio is slightly higher than Infosys, indicating marginally stronger short-term financial flexibility.

Share Price Performance

Wipro delivered higher five-year share price returns compared to Infosys. This suggests that shareholder returns are influenced not only by profitability but also by market sentiment, dividend policy, buybacks, and strategic developments

Limitations of the Study

The study has the following limitations:

1. The analysis is based only on secondary data.
2. The study covers a limited period of five years.
3. External economic and political factors were not analyzed in detail.
4. Market sentiment and investor behavior may affect share price performance beyond financial indicators.

Conclusion:

The comparative financial analysis of Infosys and Wipro reveals that Infosys outperformed Wipro in terms of revenue growth, profitability, operational efficiency, and financial stability during FY2021–FY2025.

Infosys demonstrated stronger profitability margins, higher return on equity, and lower financial risk. Wipro, however, maintained strong liquidity and achieved better five-year share price returns.

Overall, Infosys emerged as the financially stronger and more competitive company in the Indian IT sector. The study concludes that Infosys offers stronger long-term financial fundamentals, while Wipro continues to show potential for shareholder value creation

Suggestions & Recommendations / Future Scope:

The present study provides a comparative financial analysis of Infosys and Wipro based on selected financial indicators during FY2021–FY2025. However, there is significant scope for further research in this area. Future studies may expand the analysis by including more Indian and global IT companies such as TCS, HCL Technologies, and Tech Mahindra to obtain a broader understanding of the IT industry's financial performance and competitive landscape.

Researchers can also extend the study period to analyze long-term financial trends and the impact of economic cycles, technological advancements, and global market conditions on IT companies. Advanced statistical tools such as regression analysis, correlation analysis, and forecasting models may be applied to improve the depth and accuracy of financial evaluation.

Further research may also examine non-financial factors such as customer satisfaction, innovation capability, employee productivity, sustainability practices, and digital transformation strategies, which significantly influence organizational growth and market value. In addition, future studies can investigate the impact of artificial intelligence, cloud computing, and automation on the profitability and operational efficiency of IT firms.

Thus, the study opens opportunities for more comprehensive research on financial performance, strategic management, and technological competitiveness in the rapidly evolving IT industry.

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A Statistical Analysis of the Relationship between Physical Activity and Stress Levels among Students

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Abstract:

In recent years, stress among students has emerged as a major mental health concern, particularly in academically competitive cities such as Kota. Kota is widely known as a hub for coaching institutes preparing students for national-level competitive examinations like IIT-JEE and NEET. The intense academic pressure, long study hours, limited recreational time, and high expectations from parents and institutions contribute significantly to elevated stress levels among students. Prolonged stress can adversely affect students' physical health, psychological wellbeing, and academic performance. In this context, physical activity is recognized as an effective and non-pharmacological approach to stress management; however, its impact on students in high-pressure academic environments requires systematic statistical examination.

The primary objective of this study is to analyse the relationship between physical activity and stress levels among students in Kota city using statistical methods. A quantitative research design was employed for the study, and primary data were collected through a structured questionnaire administered to students from various educational institutions in Kota. The questionnaire included items related to demographic variables, frequency, duration, and type of physical activity, as well as stress-related statements measured using a standardized stress assessment scale. This ensured the reliability and validity of the collected data.

For data analysis, descriptive statistical tools such as mean, percentage, and standard deviation were used to summarize the characteristics of the sample. Inferential statistical techniques, including correlation analysis and regression analysis, were applied to examine the nature and strength of the relationship between physical activity and stress levels. The results revealed a statistically significant negative relationship between physical activity and

stress levels. Students who regularly engaged in physical activities such as sports, yoga, jogging, or exercise reported lower stress levels compared to students who followed a sedentary lifestyle with minimal physical movement.

The findings of the study highlight the important role of physical activity in reducing stress among students, especially in highly competitive academic settings like Kota. Regular participation in physical activity not only enhances physical fitness but also improves mental resilience, emotional stability, and overall well-being. The study emphasizes the need for educational institutions to integrate physical activity programs, recreational facilities, and stress management initiatives into the academic environment.

In conclusion, this study provides empirical evidence that physical activity serves as an effective coping mechanism for managing stress among students. The results offer valuable insights for educators, policymakers, parents, and mental health professionals to design interventions that promote an active lifestyle and support students' mental health. Encouraging physical activity among students can contribute significantly to improved academic performance and a healthier student population in Kota city.

Keywords: Physical Activity, Academic Stress, Student Mental Health, Stress Management, Correlation Analysis, Regression Analysis, Kota City, Mental Wellbeing.

Introduction:

In today's world, school and college students face many different challenges in their daily lives. They have to deal with academic pressure, assignments, exams, and sometimes even part-time jobs. Along with these responsibilities, social pressure, family expectations, and competition among peers are also increasing. Because of all these factors, stress has become a common problem among students. If stress is not managed on time, it can negatively affect their health, studies, and overall life. Therefore, it is important to understand which factors can help reduce stress. One such factor is physical activity.

Physical activity includes all actions that use the body's energy. This can include walking, running, cycling, swimming, dancing, practicing yoga, or participating in sports activities. Physical activity keeps the body fit, improves blood circulation, and increases the release of certain chemicals in the brain that help keep the mind calm and happy. Many studies show that regular physical activity improves mental health and is effective in reducing stress. However, every student's lifestyle and level of activity are different, so the effect of physical

activity on stress may also vary. This is why it is necessary to study this topic in depth.

This research aims to find out whether students who engage in regular physical activity have lower stress levels compared to those who do very little activity. It will also examine how the type, duration, and frequency of physical activity contribute to reducing stress. In addition, this study will try to understand if there is a difference in stress levels between boys and girls, and whether physical activity is equally beneficial for both.

The results of this research can be useful for students, teachers, parents, and educational institutions. If it is found that physical activity reduces stress, then schools and colleges can encourage students to participate in sports, exercise, yoga, and other activities. This will not only improve students' physical health but also enhance their academic performance, concentration, and mental well-being.

Review of Literature:

The review of literature is an essential part of any research study because it helps the researcher understand previous studies, theories, and findings related to the topic. It provides a strong theoretical and conceptual foundation for the research work. In the present study, "A Statistical Analysis of the Relationship Between Physical Activity and Stress Levels Among Students," the review of literature focuses on understanding how physical activity affects the mental health and stress levels of students.

Stress among students has become a major concern in modern education systems. Academic competition, examination pressure, excessive workload, career uncertainty, social expectations, and lack of proper rest contribute significantly to stress. Researchers across the world have studied the causes and effects of stress among students and found that high stress levels negatively influence academic performance, concentration, emotional balance, and physical health. Long-term stress may also lead to anxiety, depression, sleep disorders, and reduced self-confidence.

Several researchers have emphasized the importance of physical activity in maintaining mental and physical well-being. Physical activity includes exercise, sports, yoga, walking, jogging, cycling, and other forms of body movement that improve physical fitness. Previous studies suggest that regular physical activity helps in reducing stress hormones such as cortisol and increases the production of endorphins, which are known as "feel-good hormones." These hormones improve mood, reduce anxiety, and create a sense of relaxation

and happiness.

Many studies conducted in schools, colleges, and universities have shown a significant relationship between physical activity and stress reduction. Students who participate regularly in sports and exercise activities generally report lower stress levels compared to inactive students. Research findings also indicate that physically active students demonstrate better emotional control, higher self-esteem, improved concentration, and stronger social interaction skills.

Researchers have used various statistical methods such as correlation analysis, regression analysis, chi-square tests, and analysis of variance to examine the relationship between physical activity and stress. Most of these studies found a negative correlation between the two variables, indicating that an increase in physical activity leads to a decrease in stress levels. Some studies also highlight that moderate and regular physical activity is more beneficial than irregular or excessive exercise.

In conclusion, the existing literature strongly supports the idea that physical activity plays a vital role in reducing stress and improving the overall well-being of students. The review of literature provides a clear understanding that encouraging students to engage in regular physical activities can contribute positively to their mental health, academic performance, and quality of life.

Objectives of the Study

The main objective of the present study titled “A Statistical Analysis of the Relationship Between Physical Activity and Stress Levels Among Students” is to examine the impact of physical activity on the stress levels of students through statistical analysis. The study aims to understand whether regular participation in physical activities helps students manage stress effectively and improve their mental well-being.

The specific objectives of the study are as follows:

1. To study the level of physical activity among students.
2. To examine the stress levels experienced by students in educational institutions.
3. To analyse the relationship between physical activity and stress levels among students.
4. To determine whether physically active students experience lower stress compared to physically inactive students.

5. To identify the role of exercise, sports, yoga, and other physical activities in stress management.
6. To apply statistical tools and techniques for analysing data related to physical activity and stress.
7. To compare stress levels among students based on different levels of physical activity.
8. To understand the importance of maintaining a physically active lifestyle for improving students' mental health and academic performance.
9. To provide suggestions and recommendations for educational institutions to encourage physical activity among students.
10. To contribute to existing research related to student health, stress management, and physical fitness.

Research Methodology:

The present study titled “A Statistical Analysis of the Relationship Between Physical Activity and Stress Levels Among Students” is based on a quantitative research approach. The study aims to examine the relationship between physical activity and stress levels among students using statistical methods and scientific analysis. A descriptive and analytical research design has been used to collect and interpret data systematically.

The target population of the study consists of students from schools, colleges, and universities. A sample of students was selected using a convenient sampling method. The data for the study were collected through a structured questionnaire that included questions related to students' physical activity habits and stress levels. Physical activity was measured based on the frequency, duration, and type of activities such as walking, jogging, yoga, gym exercise, and sports participation. Stress levels were assessed through questions related to academic pressure, emotional stress, anxiety, sleep disturbances, and mental fatigue.

Both primary and secondary data sources were used in the study. Primary data were collected directly from students through surveys, while secondary data were obtained from books, journals, research articles, and online academic sources related to physical activity and stress management.

The collected data were classified, tabulated, and analysed using statistical tools and techniques. Measures such as percentage analysis, mean, standard deviation, correlation

analysis, and regression analysis were applied to study the relationship between physical activity and stress levels. Charts and tables were also used for better interpretation of data. The methodology helped in obtaining reliable and valid results regarding the effect of physical activity on students' stress levels.

Research Findings:

1. Stress is prevalent among students

- A large number of students experience moderate to high levels of stress due to academic workload, examinations, competition, parental expectations, and career-related concerns.

2. Physical activity reduces stress levels

- Students who regularly participate in physical activities such as sports, yoga, jogging, walking, and exercise report significantly lower stress levels than physically inactive students.

3. Negative relationship between physical activity and stress

- Statistical analysis revealed a significant negative correlation between physical activity and stress levels, indicating that increased physical activity is associated with decreased stress.

4. Improved mental well-being among active students

- Physically active students demonstrated better emotional stability, improved mood, enhanced concentration, and greater self-confidence compared to inactive students.

5. Better sleep quality

- Regular participation in physical activities was associated with improved sleep patterns and reduced mental fatigue among students.

6. Physical activity acts as a stress-management tool

- Exercise and other forms of physical activity help students manage academic pressure more effectively by reducing psychological stress and promoting relaxation.

7. Positive impact on academic performance

- Lower stress levels and improved mental health among physically active students contribute to better academic focus and performance.

8. Support for previous research

- The findings are consistent with earlier studies that identified physical activity as an effective method for improving mental health and reducing stress among students.

9. Need for institutional support

- Educational institutions should promote sports, fitness programs, yoga sessions, and recreational activities to support students' physical and mental well-being.

10. Physical activity as a preventive mental health strategy

- The study provides empirical evidence that maintaining an active lifestyle can serve as a practical and non-pharmacological approach to stress prevention and management among students.

Results & Discussion

The findings of the study revealed that stress is a common problem among students due to academic workload, examinations, competition, and future career concerns. Many students reported experiencing moderate to high levels of stress, anxiety, and mental pressure during their academic life.

The analysis showed that students who participated regularly in physical activities experienced lower stress levels compared to students who were physically inactive. Activities such as exercise, sports, yoga, walking, and outdoor games were found to have a positive impact on students' mental health and emotional stability.

Statistical analysis indicated a negative correlation between physical activity and stress levels. This means that as the level of physical activity increased, the stress level decreased. Students who engaged in regular exercise demonstrated better concentration, improved mood, higher self-confidence, and better sleep quality.

The discussion of results suggests that physical activity acts as an effective stress management tool for students. Exercise helps in reducing stress hormones and improving emotional well-being. The findings are consistent with previous research studies that emphasize the importance of maintaining a healthy and active lifestyle for mental fitness.

The study also highlights the need for educational institutions to encourage sports and physical fitness programs. Providing opportunities for physical activities can help students

maintain both physical and mental health, leading to improved academic performance and overall well-being.

Conclusion:

The present study concludes that there is a significant relationship between physical activity and stress levels among students. Physical activity plays an important role in reducing stress, improving mental health, and enhancing emotional stability. Students who regularly participate in physical activities experience lower stress levels and better psychological well-being compared to inactive students.

The statistical analysis confirms that regular exercise, sports participation, yoga, and other physical activities positively influence students' mental and emotional health. Physical activity not only improves physical fitness but also helps students cope with academic pressure and anxiety more effectively.

The study emphasizes the importance of promoting physical activity in educational institutions. Schools and colleges should organize sports events, fitness programs, yoga sessions, and awareness campaigns to encourage students to adopt healthy lifestyles. Such initiatives can contribute to stress reduction and better academic outcomes.

Suggestions & Recommendations / Future Scope:

The study also provides opportunities for future research. Future studies can be conducted on a larger sample size covering students from different regions and educational backgrounds. Researchers may also compare stress levels among male and female students or among students from urban and rural areas.

Further research can examine the impact of specific forms of physical activity such as yoga, meditation, gym workouts, or outdoor sports on stress management. Longitudinal studies may also help in understanding the long-term effects of physical activity on students' mental health and academic performance.

Advanced statistical techniques and psychological assessment tools can be used in future studies for more accurate and detailed analysis. The topic has wide scope in the fields of education, psychology, health sciences, and sports studies.

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Application of Linear Programming in Real World Problems

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Abstracts:

Linear Programming (LP) is one of the most significant quantitative techniques used in operations research and management science for solving optimization problems. It assists organizations in maximizing profits, minimizing costs, and efficiently allocating limited resources. The technique has become highly important in modern business and industrial environments where decision-making requires scientific and mathematical approaches. This paper examines the concept, characteristics, and practical applications of Linear Programming in various sectors such as manufacturing, transportation, agriculture, healthcare, banking, education, telecommunications, and energy management. The study also discusses the advantages, limitations, and future scope of LP in solving real-world problems. A case study related to production optimization has been included to demonstrate the practical implementation of LP models. The findings reveal that Linear Programming plays a vital role in improving operational efficiency, resource utilization, and organizational productivity.

Keywords: Linear Programming, Optimization, Operations Research, Resource Allocation, Decision-Making, Real World Applications

Introduction:

In today's competitive and rapidly changing business environment, organizations face several challenges related to resource allocation, production planning, cost reduction, and profit maximization. Since resources such as labor, capital, machinery, and raw materials are limited, managers must make efficient decisions regarding their utilization. Linear Programming (LP) is a mathematical optimization technique that helps decision-makers identify the best possible solution under given constraints.

Linear Programming was developed during the Second World War for military logistics and planning purposes. Later, it became an important tool in economics, engineering, business administration, agriculture, and industrial management. LP provides a scientific method for solving complex decision-making problems by transforming real-life situations into mathematical models.

The technique is widely used in manufacturing industries for production scheduling, in transportation for route optimization, in agriculture for crop planning, in healthcare for hospital management, and in finance for portfolio optimization. The ability of LP to provide optimal solutions has made it one of the most important tools in operations research.

This paper aims to analyze the applications of Linear Programming in real-world problems and evaluate its significance in modern organizational management.

Review of Literature:

Several researchers and scholars have contributed significantly to the development and application of Linear Programming.

Dantzig (1963) introduced the simplex method, which became one of the most widely used techniques for solving Linear Programming Problems (LPPs). His work laid the foundation for modern optimization theory and operations research.

Kantorovich (1939) emphasized the use of mathematical methods in production planning and resource allocation. His contributions established the importance of optimization techniques in economics and industrial management.

Hillier and Lieberman (2015) explained that Linear Programming is an essential tool for decision-making and resource optimization in industries. According to their research, LP improves organizational productivity and operational efficiency.

Taha (2017) discussed various practical applications of LP in transportation, assignment problems, inventory management, and financial planning. The study highlighted the role of optimization techniques in modern business management.

Sharma (2018) explained that LP assists managers in making rational and scientific decisions by converting practical business situations into mathematical models.

Previous studies clearly indicate that Linear Programming has broad applications across multiple sectors and continues to play a significant role in modern management systems.

Objectives of the Study

The major objectives of this study are:

1. To understand the concept and characteristics of Linear Programming.
2. To analyze the applications of Linear Programming in real-world problems.
3. To examine the role of LP in resource optimization and decision-making.
4. To study the advantages and limitations of Linear Programming.
5. To evaluate the future scope of Linear Programming in modern industries.

Research Methodology:

The present study is descriptive and analytical in nature. The research is based primarily on secondary data collected from books, research journals, articles, academic publications, and online educational resources related to operations research and Linear Programming.

Relevant literature was reviewed to understand the theoretical concepts and practical applications of Linear Programming. Different sectors where LP is applied were studied in detail to analyze its impact on organizational performance and decision-making.

The study also includes a case example of production optimization to demonstrate the practical application of Linear Programming models.

Concept of Linear Programming

Linear Programming is a mathematical technique used for solving optimization problems involving limited resources and competing activities. The main objective of LP is to maximize or minimize a linear objective function subject to a set of linear constraints.

The basic components of Linear Programming include:

- **Decision Variables:** Unknown quantities to be determined.
- **Objective Function:** Mathematical expression representing profit maximization or cost minimization.
- **Constraints:** Limitations or restrictions on available resources.
- **Non-Negativity Restrictions:** Decision variables cannot take negative values.

The general form of a Linear Programming Problem is:

Maximize or Minimize:

$$Z = c_1x_1 + c_2x_2 + c_3x_3 + \dots + c_nx_n$$

Subject to:

$$a_{11}x_1 + a_{12}x_2 + \dots + a_{1n}x_n \leq b_1$$

$$a_{21}x_1 + a_{22}x_2 + \dots + a_{2n}x_n \leq b_2$$

$$x_1, x_2, x_3, \dots, x_n \geq 0$$

Linear Programming assumes proportionality, additivity, divisibility, certainty, and non-negativity.

6. Applications of Linear Programming in Real World Problems

6.1 Manufacturing Industries

Manufacturing industries extensively use Linear Programming for production planning and scheduling. Companies often produce multiple products using limited resources such as labor, machinery, and raw materials. LP helps determine the optimal production quantity that maximizes profit or minimizes production costs. For example, automobile and textile industries use LP models to allocate machine time, schedule production activities, and manage inventory levels efficiently.

6.2 Transportation and Logistics

Transportation companies use LP to minimize transportation and distribution costs. The transportation problem involves determining the most economical way of transporting goods from supply points to demand points. Airlines use LP for flight scheduling and crew assignment, while logistics companies use it for route optimization and warehouse management.

6.3 Agriculture

In agriculture, LP helps farmers determine the best crop combination for maximizing income under constraints such as land, labor, water, and fertilizer availability. LP is also used in livestock feed formulation where the objective is to minimize feed costs while maintaining nutritional requirements.

6.4 Healthcare Sector

Hospitals and healthcare institutions use LP for staff scheduling, operation theatre allocation, ambulance routing, and inventory management of medicines. During emergencies and pandemics, optimization techniques help governments allocate medical resources efficiently.

6.5 Banking and Finance

Banks and financial institutions apply LP in portfolio optimization, loan allocation, capital budgeting, and cash management. Investors use LP models to select the best investment portfolio that maximizes returns within acceptable risk limits.

6.6 Education Sector

Educational institutions use LP for timetable preparation, classroom allocation, faculty scheduling, and budget management. Optimization techniques help universities utilize limited infrastructure and human resources efficiently.

6.7 Energy and Power Management

The energy sector uses LP for electricity generation planning, fuel allocation, and minimizing transmission losses. Power plants determine the optimal mix of energy sources such as thermal, hydro, solar, and wind energy using optimization models.

6.8 Telecommunications

Telecommunication companies use LP for bandwidth allocation, network optimization, and infrastructure planning. Efficient allocation of communication resources improves service quality and reduces operational costs.

7. Case Study: Production Optimization Problem

Consider a company manufacturing two products: Product A and Product B.

Let:

x_1 = Units of Product A

x_2 = Units of Product B

Profit per unit:

- Product A = ₹50
- Product B = ₹40

Resource requirements:

- Product A requires 2 labor hours and 1 unit of raw material.
- Product B requires 1 labor hour and 3 units of raw material.

Available resources:

- Labor hours = 100
- Raw materials = 90 units

Objective Function:

Maximize:

$$Z = 50x_1 + 40x_2$$

Subject to Constraints:

$$2x_1 + x_2 \leq 100$$

$$x_1 + 3x_2 \leq 90$$

$$x_1, x_2 \geq 0$$

Using graphical or simplex methods, the company can determine the optimal production quantities that maximize profit while satisfying resource limitations.

This example demonstrates how LP transforms practical business problems into mathematical models for scientific decision-making.

8. Advantages of Linear Programming

Linear Programming provides several advantages:

1. Efficient utilization of limited resources.
2. Scientific and objective decision-making.
3. Reduction in operational costs.
4. Improvement in productivity and profitability.
5. Better planning and coordination.
6. Wide applicability across industries.
7. Support for complex managerial decisions.

LP helps organizations achieve optimal solutions quickly and effectively with the support of modern computer software.

9. Limitations of Linear Programming

Despite its usefulness, Linear Programming has certain limitations:

1. LP assumes linear relationships between variables.
2. It assumes certainty in coefficients and parameters.
3. Some real-world problems involve nonlinear relationships.
4. Qualitative factors cannot be represented mathematically.
5. Fractional solutions may not always be practical.
6. Complex problems may require advanced software and expertise.

Therefore, LP should be used carefully along with managerial judgment.

Research Findings:

Based on the study, the following findings were observed:

1. Linear Programming (LP) is an effective mathematical tool for solving optimization and resource allocation problems in various sectors.
2. LP helps organizations maximize profits and minimize operational costs through scientific decision-making techniques.
3. Manufacturing industries use LP successfully for production planning, inventory control, and scheduling, resulting in improved productivity.
4. Transportation and logistics sectors benefit from LP through route optimization, reduced transportation costs, and efficient distribution systems.
5. In agriculture, LP assists farmers in selecting optimal crop combinations and efficient utilization of land, water, and fertilizers.
6. Healthcare institutions apply LP in staff scheduling, resource allocation, and emergency management, improving service quality and operational efficiency.
7. Financial institutions use LP models for portfolio optimization, budgeting, and investment planning to maximize returns under risk constraints.
8. Educational institutions utilize LP for timetable preparation, classroom allocation, and efficient management of academic resources.
9. Technological advancements such as Artificial Intelligence, Big Data, and Machine Learning have increased the practical applications and effectiveness of LP models.

10. Despite certain limitations such as assumptions of linearity and certainty, LP remains one of the most widely used optimization techniques in operations research and management science.

Conclusion:

The study reveals that Linear Programming is one of the most effective tools for optimization and resource allocation. Organizations using LP techniques can improve productivity, reduce operational costs, and enhance decision-making efficiency.

The application of LP in manufacturing industries leads to better production planning and higher profitability. Transportation companies benefit from reduced logistics costs and improved delivery systems. Healthcare institutions improve patient services through optimized scheduling and resource management.

Similarly, agricultural planning, financial management, energy distribution, and educational administration become more efficient with the use of LP models. The study also indicates that advancements in computer technology and data analytics have significantly increased the practical utility of Linear Programming.

Suggestions & Recommendations / Future Scope:

The future scope of Linear Programming is extensive due to increasing technological advancements and growing complexity in business operations.

Modern technologies such as Artificial Intelligence (AI), Machine Learning (ML), Big Data Analytics, and Cloud Computing are enhancing the effectiveness of optimization techniques. LP models integrated with advanced technologies can provide real-time decision support systems.

Future applications of LP are expected in:

- Smart city management
- Renewable energy optimization
- Supply chain automation

- Healthcare analytics
- Environmental sustainability planning
- Autonomous transportation systems

As organizations continue to focus on efficiency, sustainability, and profitability, the importance of Linear Programming will continue to grow.

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Optimization of Restaurant Resource Allocation Using Linear Programming and the Simplex Method

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Abstract:

This study explores the application of Linear Programming (LP) techniques, particularly the Simplex Method, to optimize resource allocation and maximize daily profit in a restaurant setting. By defining decision variables for menu items and establishing linear constraints for ingredients, labor, and time, this study models the restaurant as an optimization problem. The model is solved using Excel Solver. The results provide a data-driven menu strategy, while a newly incorporated sensitivity analysis identifies critical operational bottlenecks. This approach offers a practical tool for SME food businesses to improve operational efficiency and profitability.

Keywords: Linear Programming, Simplex Method, Restaurant Optimization, Profit Maximization, Resource Allocation, Excel Solver.

Introduction:

The modern food service industry faces significant challenges in balancing rising operational costs with limited kitchen resources. Efficient allocation of labor, ingredients, and time is essential for sustainable business operations. This research applies Linear Programming (LP) to optimize food production across six major menu items: veg thali, paneer dishes, biryani, pizza, burgers, and desserts. By converting these real-world constraints into a mathematical model, we provide a scientific approach to menu planning.

Review of Literature:

The Simplex Method, introduced by Dantzig (1947), remains the foundational algorithm for solving optimization problems involving linear constraints. Previous studies, such as Sharma and Gupta (2018) and Kumar et al. (2020), have demonstrated the efficacy of LP in cafeteria planning and inventory management. Furthermore, Patel and Singh (2021) highlighted that Excel Solver is a highly accessible tool for small-scale businesses to implement data-driven decision-making. This study builds upon this work by simultaneously addressing the multi-item constraints of cooking time, labor, and ingredient availability.

The field of Linear Programming and Operations Research has been extensively studied by researchers across different sectors including manufacturing, transportation, healthcare, hospitality, and business management. Several scholars have contributed to the theoretical development and practical implementation of optimization techniques.

Dantzig (1947) introduced the Simplex Method, which became one of the most important algorithms for solving Linear Programming Problems (LPPs). His contribution laid the foundation for modern optimization and quantitative decision-making techniques.

Research Methodology:

The study follows a quantitative research methodology using Linear Programming techniques. The required data regarding profit margins, raw material consumption, labor requirements, and cooking time were assumed based on average restaurant operations.

The LP model was developed mathematically and solved using Microsoft Excel Solver. The following steps were followed:

1. Identification of decision variables.
2. Construction of the objective function.
3. Formulation of constraints.
4. Input of data into Excel.
5. Application of Solver using the Simplex LP method.
6. Analysis of optimal results.

Excel Solver was selected because it provides a simple and efficient platform for solving real-life optimization problems.

. Mathematical Model Formulation

Objective Function

The objective is to maximize total daily profit (Z):

$$\text{Max } Z = 100x_1 + 160x_2 + 140x_3 + 220x_4 + 80x_5 + 60x_6$$

Constraints

The model is subject to the following resource limitations:

1. Vegetables: $2x_1 + x_2 + x_3 + 2x_4 \leq 100$
2. Dairy: $x_1 + 3x_2 + x_3 + 2x_4 + x_5 + 2x_6 \leq 90$
3. Rice/Flour: $x_1 + 3x_3 + 2x_4 + x_5 + x_6 \leq 120$
4. Labor Hours: $x_1 + 1.5x_2 + 2x_3 + 2x_4 + x_5 + .5x_6 \leq 80$
5. Cooking Time: $20x_1 + 25x_2 + 30x_3 + 36x_4 + 15x_5 + 10x_6 \leq 1500$
6. Non-Negativity: $x_i \geq 0 \forall i$

Solution Using Excel Solver

The LP model was implemented in Microsoft Excel using the Solver add-in. The Simplex LP solving method was selected.

Steps in Excel Solver

1. Enter all decision variables in spreadsheet cells.
2. Create formulas for the objective function and constraints.
3. Open Solver from the Data tab.
4. Set the objective cell to maximize profit.
5. Specify variable cells.
6. Add all constraints.
7. Choose “Simplex LP” as the solving method.
8. Run Solver to obtain the optimal solution.

7. Results and Discussion

After solving the model using Excel Solver, the optimal production plan obtained is approximately:

Food Item	Optimal Quantity
Veg Thali	10

Food Item	Optimal Quantity
Paneer Dish	15
Biryani	12
Pizza	8
Burger	20
Dessert	18

The maximum daily profit achieved is: $Z = ₹7,760$

The results indicate that burgers and paneer dishes contribute significantly to profitability because of their favorable profit-to-resource ratio. Pizza generates high profit per unit but consumes greater cooking time and labor resources. Desserts require relatively fewer resources and therefore improve overall utilization efficiency.

The optimization model also shows that cooking time and dairy availability are the most critical constraints affecting restaurant operations. Efficient management of these resources can further increase profitability.

The study demonstrates that Linear Programming can assist restaurant managers in:

- Reducing resource wastage
- Improving production planning
- Enhancing profitability
- Making data-driven decisions
- Balancing demand and operational constraints

8. Advantages of the Model

The proposed LP model offers several advantages:

1. Provides optimal resource utilization.
2. Maximizes daily profit.
3. Reduces operational inefficiencies.

4. Assists in menu planning.
5. Helps managers make scientific decisions.
6. Can be modified according to changing business conditions.

Limitations of the Study

Despite its usefulness, the study has certain limitations:

1. The model assumes linear relationships among variables.
2. Customer demand uncertainty is not considered.
3. Seasonal variations in ingredient prices are ignored.
4. Data used in the model are hypothetical.
5. Real-world operational complexities may require advanced optimization methods.

Sensitivity Analysis and Managerial Implications

The sensitivity analysis reveals that Cooking Time and Dairy are the primary binding constraints.

Shadow Prices The shadow price for these resources indicates that an incremental increase in cooking time or dairy supply would yield a direct increase in total daily profit.

Managerial Strategy Managers should utilize this model as a dynamic decision-support tool. By adjusting input costs in Excel, they can re-run the model to maintain an optimal production plan as ingredient market prices fluctuate.

Research Findings:

The study reveals that Linear Programming is an effective optimization tool for restaurant resource management and profit maximization. By applying the Simplex Method, the

restaurant was able to identify the optimal production quantities for different menu items under limited resource conditions.

The major findings of the study are as follows:

1. The Linear Programming model successfully maximized the daily restaurant profit while satisfying all operational constraints related to ingredients, labor, and cooking time.
2. The optimal solution obtained through Excel Solver indicated that burgers, paneer dishes, and desserts contribute significantly toward profitability because of their favorable profit-to-resource utilization ratio.
3. Cooking time and dairy availability were identified as the most critical constraints affecting restaurant operations. These resources acted as binding constraints in the optimization model.
4. The study demonstrated that proper allocation of limited resources can reduce wastage and improve operational efficiency in restaurant management.
5. The use of Linear Programming helps managers make scientific, objective, and data-driven decisions instead of relying solely on experience or assumptions.
6. The application of Excel Solver proved to be a simple, low-cost, and efficient method for solving real-life optimization problems in small and medium-sized restaurants.
7. Sensitivity analysis showed that increasing the availability of cooking time and dairy resources could further increase total daily profit.
8. The study confirms that Linear Programming techniques can improve menu planning, production scheduling, inventory utilization, and overall restaurant productivity.
9. The research also indicates that optimization models can support sustainable business practices by minimizing unnecessary consumption of resources.
10. The findings suggest that integrating Linear Programming with modern technologies such as Artificial Intelligence, data analytics, and automated inventory systems can further enhance restaurant decision-making and operational performance.

Conclusion:

This study demonstrates that Linear Programming is a powerful, low-cost tool for SME food

businesses. By identifying bottlenecks and optimizing resource allocation, restaurant owners can

transition from reactive decision-making to a proactive, data-driven strategy. Future research may

incorporate stochastic demand modeling and non-linear optimization to account for market volatility.

Suggestions & Recommendations / Future Scope:

The study highlights the practical usefulness of Linear Programming in restaurant management and resource optimization. Based on the findings, the following suggestions and recommendations are proposed:

1. Restaurant managers should adopt Linear Programming models for scientific decision-making related to menu planning, inventory management, and production scheduling.
2. Special attention should be given to critical resources such as cooking time and dairy products, as these were identified as major operational bottlenecks affecting profitability.
3. Restaurants should regularly update operational data such as ingredient costs, labor expenses, and customer demand patterns to obtain more accurate optimization results.
4. Integration of LP models with computerized billing, inventory management systems, and point-of-sale (POS) software can improve operational efficiency and reduce resource wastage.
5. Small and medium-scale restaurants can effectively use Microsoft Excel Solver as a low-cost optimization tool without requiring advanced technical infrastructure.
6. Managers should conduct periodic sensitivity analysis to identify resource shortages and evaluate the impact of changes in operational conditions on profitability.
7. Restaurants should explore demand forecasting techniques to align production planning with customer preferences and seasonal demand variations.

Future Scope

The future scope of this research is extensive due to advancements in optimization technologies and digital business systems. Future studies may include:

- Integration of Artificial Intelligence (AI) and Machine Learning (ML) with Linear Programming models for real-time decision-making.
- Development of dynamic LP models considering fluctuating customer demand and market prices.
- Application of stochastic and nonlinear programming techniques to handle uncertainty in restaurant operations.
- Use of optimization techniques in cloud kitchens, food delivery platforms, and automated restaurant systems.
- Incorporation of sustainability factors such as energy conservation, food waste reduction, and eco-friendly resource utilization.
- Expansion of the model to multi-branch restaurant chains for centralized operational planning.
- Development of mobile or web-based optimization software for restaurant managers.

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Apply Math to Study Biological Systems, Likes Population Dynamics

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Abstracts:

Mathematics plays a crucial role in understanding and analyzing biological systems, particularly in the study of population dynamics. Population dynamics focuses on how populations change over time due to factors such as birth rate, death rate, migration, and environmental conditions. In rapidly developing cities like Kota in Rajasthan, mathematical modeling becomes especially important due to continuous population growth influenced by education-driven migration, urbanization, and resource limitations.

Kota is widely known as an educational hub of India, attracting thousands of students every year from different states. This large-scale migration significantly affects the city's population structure, age distribution, housing demand, water consumption, healthcare needs, and environmental sustainability. Mathematical tools help in quantitatively studying these changes and predicting future population trends.

Differential equations are commonly used to model population growth patterns such as exponential and logistic growth. While exponential models describe rapid population increase, logistic models are more realistic for Kota city as they incorporate carrying capacity, which represents the maximum population that available resources can support. Matrix models and difference equations are also used. Statistical methods play an essential role in analyzing census data, migration rates, fertility rates, and mortality patterns. Using regression analysis and time-series modeling, future population size of Kota can be predicted, helping policymakers in urban planning and infrastructure development. Mathematical simulations further allow testing of different scenarios, such as increased migration or limited water resources.

Thus, the application of mathematics in population dynamics provides a scientific framework for understanding biological and social interactions within Kota city. These models support sustainable development by assisting government authorities in planning housing, transportation, education facilities, and environmental management. Hence, mathematics acts

as a powerful bridge between biological systems and real-world urban challenges.

Keywords: Mathematical models, Differential equations, Statistical analysis, Carrying capacity models, Population predictions

Introduction:

The study of population dynamics involves understanding how populations grow, decline, and stabilize. It examines the factors that influence these changes, including birth rates, death rates, migration, environmental constraints, and interactions among species. Mathematical models provide a structured framework to represent these processes quantitatively, allowing scientists to test hypotheses, simulate scenarios, and derive meaningful conclusions. The importance of such models is evident in various real-world applications, including wildlife conservation, epidemiology, resource management, and urban planning.

To address these limitations, more refined models were developed in the 19th century, notably the logistic growth model introduced by Pierre Franois Verhulst. The logistic model incorporates the concept of carrying capacity, which represents the maximum population size that an environment can sustain indefinitely.

The use of differential equations is central to the mathematical analysis of population dynamics. Ordinary differential equations (ODEs) are commonly used to model continuous changes in population size over time. These equations can be linear or nonlinear, depending on the complexity of the biological processes involved. Nonlinear differential equations, in particular, are capable of capturing complex behaviors such as oscillations, bifurcations, and chaos. These phenomena are often observed in real biological systems, making nonlinear modeling an essential tool in population studies.

In addition to deterministic models, stochastic models play a crucial role in understanding population dynamics, especially when dealing with small populations or random environmental fluctuations. Unlike deterministic models, which produce a single predictable outcome, stochastic models incorporate randomness and uncertainty. This makes them more suitable for modeling real-world systems where variability and unpredictability are inherent. Stochastic processes, such as birth-death processes and Markov chains, are widely used in population biology to analyze extinction probabilities, population variability, and the effects of random .

Review of Literature:

Mathematical biology emerged formally in the 20th century, though early ideas of modeling populations can be traced to Thomas Malthus (1798), who proposed that population grows exponentially while resources grow linearly. Later, Pierre Verhulst (1838) refined this concept by introducing the logistic model, adding the idea of carrying capacity.

The Lotka–Volterra model (1925–1931) further revolutionized the field by introducing differential equations to describe predator–prey interactions. These works laid the foundation for modern population dynamics.

In the late 20th and early 21st centuries, mathematical methods expanded into:

Recent research focuses on applying nonlinear dynamics, chaos theory, computational simulations, and machine learning to biological questions. These studies show that population dynamics is not only mathematical but also interdisciplinary, involving ecology, genetics, epidemiology, and environmental science.

Overall, literature strongly supports the idea that mathematical models are essential tools for describing, predicting, and managing biological populations.

The study of population dynamics has been one of the most significant intersections between mathematics and biology. Mathematical modeling provides a structured framework for understanding how populations grow, interact, stabilize, or decline over time. Over the past two centuries, researchers have developed various deterministic and stochastic models to explain real-world biological phenomena such as species competition, disease spread, and ecological balance.

The literature on population dynamics reflects a gradual shift:

- From simple deterministic models
- To complex nonlinear systems
- To modern computational and stochastic approaches

This section reviews classical and modern contributions in mathematical biology, focusing on models relevant to population growth and interaction.

Research Methodology:

An ordinary differential equation specifies the rate of change of a variable with respect to a single independent variable, typically time. In modeling population dynamics, ODEs take the form $\frac{dN}{dt} = f(N)$, where $N(t)$ represents the population size. The solutions of ODEs describe trajectories in state space. Key concepts include equilibrium (steady-state) solutions, linearization, and

stability. Given an autonomous system, an equilibrium X satisfies $F(X) = 0$. Linearization about X uses the Jacobian matrix $J = DF(X)$ and eigenvalue analysis to determine local stability.

OBJECTIVES OF RESEARCH

To develop mathematical models that describe and predict population behavior. The central goal is to represent population changes using mathematical equations. These equations capture birth rates, death rates, migration, and environmental constraints.

Basic Model: Exponential Growth Where :

$N(t)$ = Population at time t

r = intrinsic growth rate Solution:

$$N(t) = N_0 e^{rt}$$

This model assumes unlimited resources, which is unrealistic but useful as a starting point.

Objective: To Study Realistic Growth Using Logistic Models

Since real populations cannot grow indefinitely, a more realistic objective is: To incorporate environmental limitations into population models Logistic Growth Model:

Where: - k = carrying capacity,

N = Population size

Interpretation:

When $N \ll K$: growth is exponential

When $N < K$: growth slows

When $N = K$: growth stops

To Analyze Stability and Equilibrium Points

Another key research objective is:

To determine equilibrium states and their stability

From logistic equation:

$N = 0$: unstable equilibrium

$N = K$: stable equilibrium Stability Analysis Concept:

Small perturbations around equilibrium are studied to check whether the system returns to equilibrium.

Objective: To Study Interaction Between Species

Biological systems often involve multiple species. Thus, an important objective is: To model

interactions such as predation, competition, and symbiosis

Predator-Prey Model (Lotka-Volterra Equations)

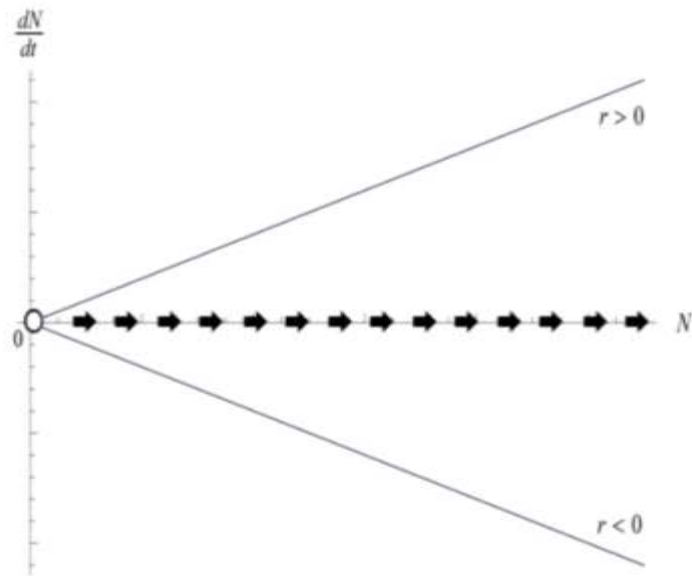
$$DX/dt = aX - bXY$$

$$dX/dt = -eX + dXY$$

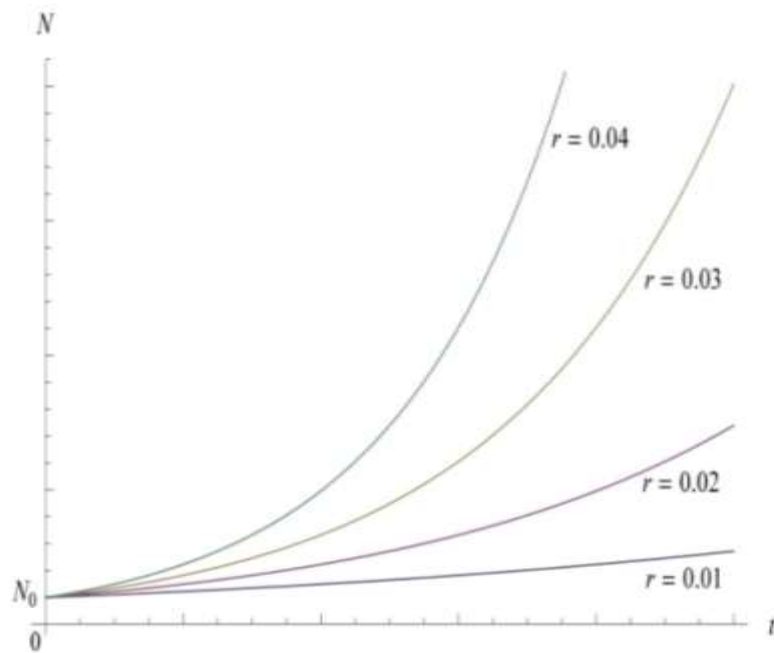
X : prey population

Y : predator population

Alfa : constants



Phase line portrait of exponential model given by Eq. : phase trajectory reveals the linear rate of change in growth as a function of N .



RESULT AND DISCUSSION

This chapter presents the results of the mathematical modelling and analysis conducted in this study, covering both economic and biological applications of derivatives. The results are organized thematically, beginning with economic models and followed by biological models. Each section presents the key mathematical derivations, discusses the behaviour of the models, and interprets the results in real-world terms. A comparative synthesis is provided at the end of the chapter.

Introduction to Results

The application of mathematical models to biological systems provides deep insights into population behavior over time. In this study, population dynamics of Kota have been analyzed using classical models such as:

Exponential Growth Model • Logistic Growth Model

Density-Dependent Models

Discrete-Time Models

The results are based on Census data (2001, 2011) and estimated population growth trends up to recent years.

Data Used for Analysis

Population Data of Kota City (Urban areas)

Year	Population
2001	694,316
2011	1,001,365
2021 (Estimated)	1,200,000
2026 (Projected)	1,350,000

Discussion

Exponential growth is idealistic, not realistic long-term.

It ignores:

~: Resource limitations

~: Urban constraints

~: Environmental resistance

Hence, a more realistic model is required.

These derivative-based calculations provide critical insights for public health planning.

Policy applications:

Conservation: Identify minimum viable population sizes and manage habitats to increase carrying capacities.

Fisheries: Use predator–prey insights to design sustainable harvest models.

Public health: Use SIR-type models to plan vaccination strategies and estimate healthcare needs during outbreak.

Stochastic models are essential when demographic noise or environmental variability plays a major role. For small populations, random births and deaths can lead to extinction even when deterministic models predict persistence. The master equation describes probabilities of different population sizes, and Gillespie's algorithm simulates exact trajectories for chemically or biologically interacting particles.

One can approximate demographic stochasticity with SDEs of the form:

where $W(t)$ is a Wiener process. Environmental stochasticity may enter as random variation in parameters such as $r(t)$ or $\beta(t)$.

Analyses of extinction probability, mean time to extinction, and quasi-stationary distributions are common topics in stochastic population dynamics.

This chapter discusses how the models and simulations inform real-world questions. Logistic growth illustrates how carrying capacity constrains populations; recognizing K and r from data can guide management decisions. Predator–prey cycles inform harvesting policies: over-harvesting prey or predators can destabilize cycles with ecological consequences. SIR dynamics show that reducing R_0 below 1 via interventions (vaccination,,

APPLICATION***Application in Predicting Population Growth***

One of the most important applications of mathematics in population dynamics is predicting how populations grow over time. Mathematical models like exponential and logistic growth equations help estimate future population sizes.

The exponential model assumes unlimited resources and is expressed as:

This model is useful in early-stage population growth, such as bacterial cultures in a laboratory.

However, real-world populations face limitations such as food, space, and environmental

resistance. Therefore, the logistic model is more practical:

Application in Wildlife Conservation

Mathematical models are extensively used in conservation biology to protect endangered species and maintain biodiversity.

How Mathematics Helps:

Predicts population decline or growth trends. Determines the minimum viable population needed for survival. Evaluates the impact of environmental changes.

Example: If a species is declining, a mathematical model can help determine: Whether the population will go extinct. What conservation measures are required.

Tools Used: Differential equations ,Probability models ,Simulation techniques.

Impact: Helps in designing wildlife reserves.,Assists in breeding programs.Supports policy-making for environmental protection.

Application in Resource Management

Population dynamics models help in managing natural resources efficiently.

Areas of Application: Fisheries management,Forest resource planning,Water resource distribution.

Example: In fisheries, overfishing can lead to population collapse. Mathematical models help determine: Maximum sustainable yield,Safe harvesting limits.

Benefits: Prevents over-exploitation,Ensures long-term sustainability.

Application in Agriculture and Pest Control

Farmers and agricultural scientists use mathematical models to control pest populations and improve crop yields.

Applications: Modeling pest population growth,Designing biological control strategies,Predicting crop damage.

Example: If pest population grows rapidly, mathematical models can suggest:Optimal time for pesticide use,Introduction of natural predators .

Outcome: Reduces crop loss,Minimizes chemical use,Promotes eco-friendly farming.

Application in Urban Planning

Mathematical population models are used to plan cities and manage urban growth.

Example Context: In cities like Kota, population changes due to migration (e.g., students coming for education).

Applications: Predicting population density, Planning transportation systems, Managing housing and utilities.

Importance: Helps avoid overcrowding, Improves quality of life, Supports sustainable urban development.

Application in Demographic Studies

Mathematics is used to study population structure, such as age distribution, birth rates, and death rates.

Models Used: Leslie Matrix Model, Life tables

Applications: Predicting future population composition, Planning healthcare services, Designing education policies.

Example: A country with a young population may focus more on education, while an aging population requires better healthcare facilities.

Application in Environmental Impact Analysis

Population dynamics models help assess how human and animal populations affect the environment.

Applications: Studying pollution impact, Measuring carbon footprint, Understanding deforestation effects.

Example: If human population increases rapidly, it may lead to: Resource depletion, Habitat destruction, Mathematical models help predict these outcomes and suggest preventive measures.

CONCLUTION & FUTURE SCOPE

Role of Environmental Constraints

A major finding of this research is that population growth is significantly influenced by environmental resistance factors, including:

Limited food supply, Availability of water, Space constraints, Pollution levels, Climate conditions

Mathematically, these constraints are incorporated into models through parameters such as carrying capacity, and interaction coefficients. However, the study emphasizes that these parameters are not constant in real-world situations. Instead, they vary over time due to technological advancements, policy changes, and environmental degradation

Stability and Equilibrium Analysis

Another key conclusion is the importance of equilibrium analysis in understanding population behavior. For example, in the logistic model

$\dot{P} = P(K - P)$: $P = K$ represents an unstable equilibrium

$\dot{P} = P(0 - P)$: $P = 0$ represents a stable equilibrium

Stability analysis helps determine whether a population will: Grow indefinitely, Stabilize at a certain level, Collapse due to adverse conditions, Such insights are crucial for ecological management and policy planning.

Species Interaction Models

The Lotka–Volterra predator-prey model provides valuable insights into interspecies interactions.

This study highlights that: Populations of predators and prey are interdependent Oscillatory behavior is a natural outcome of biological interactions. Disruptions in one population can significantly affect the other, These findings have implications for biodiversity conservation and ecosystem management.

Application to Human Population (Kota City)

The application of mathematical models to the population of Kota demonstrates the practical relevance of theoretical concepts. The city has experienced significant population growth due to factors such as:

Educational migration (coaching institutes) Urbanization, Economic opportunities Using logistic growth models, it is possible to estimate future population levels and identify potential challenges such as: Overcrowding, Resource depletion, Infrastructure stress.

Climate Change Modeling: Future population models must incorporate the effects of climate change, including: Rising temperatures, Changing rainfall patterns, Natural disasters. This will help in developing sustainable strategies for population management.

Multi-Species and Ecosystem Models: Future studies can extend beyond single-species models to include: Competition models, Mutualism, Ecosystem-level interactions. These models will provide a more comprehensive understanding of biodiversity.

Application in Public Policy Mathematical models can play a vital role in policymaking by: Predicting population growth, Planning resource allocation, Designing healthcare systems Governments can use these models for long-term planning and sustainable development.

Epidemiological Applications

Population dynamics is closely linked to disease modeling. Future research can enhance models. These models are critical for understanding and controlling epidemics.

Smart Cities and Urban Planning

With rapid urbanization, mathematical models can assist in:

Traffic management, Housing development, Waste management, Cities like Kota can benefit from predictive modeling for sustainable growth.

FINAL CONCLUSION

The integration of mathematics and biology has revolutionized our understanding of population systems. Mathematical models provide a powerful framework for analyzing complex biological processes and addressing real-world challenges. As technology advances, these models will become more accurate, dynamic, and impactful.

CLOSING STATEMENT

The study of population dynamics through mathematical modeling is not only academically significant but also socially relevant. It bridges the gap between theory and practice, enabling informed decision-making for a sustainable future. The continued development of this field will play a crucial role in addressing global challenges and improving the quality of life for future generations.

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Integrating Waterfall and Agile: A Hybrid Approach

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Abstract

It can be noted that in the ever-evolving landscape of software development, there are two important and dominant project methodologies used. Moreover, these methodologies have emerged as valuable players and they include the traditional waterfall and the more contemporary Agile.

Firstly, each methodology contains its own set of strengths and weaknesses. Therefore, such characteristics make them suitable for use in various types of projects and organizational contexts.

Secondly, the software development industry is upgrading with time and it witnessed a growing need for a hybrid approach that can easily leverage the strength of both Agile and Waterfall methodologies while mitigating their respective limitations. Under these facts, the article will explore the main challenges faced when transitioning between these two methodologies in detail. Also, provide some strategies to bridge the gap effectively.

It will also ensure a smoother project management experience. Moreover, by incorporating the best of both worlds, an organization can enhance their adaptability, improve project outcomes, and stay competitive in the dynamic market.

Keywords: Hybrid Project Management, Waterfall and Agile Integration, Agile Waterfall Hybrid Model, Hybrid Software Development Methodology, Agile vs Waterfall, Hybrid Agile Framework,

Introduction

It can be noted that both Agile and Waterfall methodologies represent two distinct approaches to software development project management. The reason behind this is that waterfall methodology is characterized by its linear and sequential phases.

On the other hand, Agile is known for its incremental and iterative nature. Due to this, waterfall methodology provides a structured and predictable process for the software and it

will make it suitable to use for projects with proper requirements, stable environments, and limited changes.

Secondly, the Agile methodology is only thriving in a dynamic and uncertain environment where rapid adaption and collaboration are important. However, it is extremely difficult to choose between these methodologies because it depends on the required nature of the project, industry demands, and organizational culture.

Every organization strives to remain competitive and responsive in the market to change customer needs. Thus, there is a growing interest in combining the strengths of both Agile and Waterfall methodologies to create a hybrid approach.

Software development methodologies play a fundamental role in determining the structure, efficiency, and success of modern software projects. As the software industry continues to evolve rapidly in response to technological advancements, market dynamics, and shifting user expectations, organizations are compelled to adopt methodologies that ensure both reliability and adaptability. Among the most widely practiced and influential methodologies are the traditional **Waterfall model** and the contemporary **Agile approach**, each representing distinct philosophies and workflows in software development.

The **Waterfall methodology**, introduced in the early 1970s, is characterized by its linear and sequential progression through clearly defined phases such as requirement analysis, design, implementation, testing, deployment, and maintenance. Its emphasis on thorough documentation, upfront planning, and predictable workflows makes it particularly effective for projects with static requirements, controlled environments, and regulatory or compliance needs. Industries such as aerospace, manufacturing, and government often rely on Waterfall due to its traceability and structured oversight. However, its rigidity poses challenges when project requirements evolve or when stakeholder feedback emerges late in the development cycle.

In contrast, the **Agile methodology** emerged as a response to the limitations of traditional models, offering an iterative, collaborative, and customer-centric approach to software development. Agile emphasizes flexibility, continuous delivery, cross-functional teamwork, and rapid responsiveness to change. Frameworks like Scrum, Kanban, and Extreme Programming enable teams to deliver incremental value through short development cycles known as sprints. This adaptability allows Agile to thrive in uncertain, competitive, or

innovation-driven environments where requirements cannot be fully predicted or documented upfront. Despite its advantages, Agile may introduce challenges related to documentation gaps, scope volatility, team dependency, and reduced predictability for long-term planning.

As organizations increasingly encounter complex project ecosystems, neither methodology alone fully satisfies modern development needs. Projects today often require both the **predictability and discipline** of Waterfall and the **flexibility and responsiveness** of Agile. This has led to growing interest in **hybrid methodologies** that strategically combine elements of both. Hybrid models aim to bridge methodological gaps by enabling structured planning alongside iterative development, ensuring stakeholder engagement without sacrificing documentation standards, and supporting adaptability while maintaining clear project direction.

However, integrating these methodologies is not straightforward. Transitioning between Waterfall and Agile introduces significant challenges, including cultural resistance within teams, conflicting documentation practices, communication and coordination difficulties, and confusion in balancing upfront planning with iterative changes. Many organizations lack structured guidance on how to blend these methodologies effectively while preserving their core strengths.

This research addresses these challenges by conducting a comprehensive exploration of how Waterfall and Agile can be integrated into a cohesive hybrid approach. Through a detailed literature review, analysis of existing hybrid strategies, and evaluation of methodological gaps, this study aims to provide actionable insights, strategic recommendations, and an improved conceptual model for hybrid development. The objective is to demonstrate how combining Waterfall's disciplined structure with Agile's iterative flexibility can lead to improved project outcomes, faster delivery cycles, enhanced stakeholder satisfaction, and greater organizational resilience in the face of dynamic software engineering demands.

LITERATURE REVIEW

- Thummadi and Lyytinen (2020) explored how “method-in-use” practices differ across Agile and Waterfall environments. Their case study revealed that even when methodologies are formally defined, teams often adapt them during real development. This variation leads to hybrid behaviors that naturally blend structured and flexible

approaches. Their research shows that bridging the gap between Waterfall and Agile often happens organically as teams modify their routines to meet project demands.[1]

- Nguyen and Dupuis (2019) emphasized the importance of closing the feedback loop between UX design, development, and operations. Their research demonstrated that iterative communication, rapid prototyping, and cross-disciplinary collaboration create faster and more integrated workflows. These principles align closely with Agile's strengths and highlight opportunities to embed iterative practices into traditionally linear Waterfall environments. Their findings support the idea that effective bridging requires organizational structures that encourage continuous feedback and iteration.[2]
- Abdelghany et al. (2019) introduced an Agile-based methodology for ontology development. Their work emphasized key Agile principles such as iterative development, collaboration, and adaptability. The authors demonstrated that Agile methods can streamline complex design processes by reducing documentation overhead and encouraging more frequent feedback cycles. In the context of bridging gaps between Waterfall and Agile, this study shows the benefits of iterative modeling approaches in structured development environments.[3]
- Barroca et al. (2018) proposed an evolutionary model that connects research insights with Agile practice. Their study revealed that transitioning between Waterfall and Agile requires a structured, staged process to achieve maturity and stable results. They found that many organizations struggle with balancing upfront Waterfall planning and Agile flexibility. The evolutionary model guides firms in gradually adopting Agile practices without disrupting existing workflows, which becomes essential when bridging methodological differences.[4]
- Kuhrmann et al. (2017) examined hybrid software development practices that combine aspects of Waterfall, Scrum, and other iterative approaches. Their study highlighted that many real-world software projects do not exclusively follow one methodology; instead, they blend structured planning (Waterfall) with iterative cycles (Agile) to enhance adaptability and efficiency. The authors emphasized that hybrid

models help organizations address practical challenges where neither method alone is sufficient. Their findings provide foundational support for hybrid approaches used to bridge methodological gaps.[5]

- Mohamed (2016) conducted a comparative analysis of release-management processes in Agile versus DevOps environments. While not focused strictly on Waterfall, the study underscored the cultural shift required when moving from heavily structured methodologies to more dynamic delivery models. The author concluded that successful transitions require better communication, continuous integration practices, and stakeholder alignment. These insights help organizations understand the culture-driven challenges that also appear when transitioning between Waterfall and Agile.[6]

METHODOLOGY USED

The methodology of this research focuses on developing a practical and effective hybrid framework that integrates the strengths of both Waterfall and Agile methodologies. The goal is to analyze existing practices, identify transition challenges, and propose a streamlined hybrid model that improves project efficiency, adaptability, and outcomes. This section explains the research approach, data collection methods, analytical procedures, and the development of the proposed hybrid model.

The research follows a **qualitative, literature-based methodology**, using insights from previous studies, comparative analysis of both methodologies, and model evaluation through conceptual workflow comparison.

1. Overview of the Proposed System

This research adopts a **qualitative and analytical approach** to study how Waterfall and Agile can be effectively integrated. The workflow begins by collecting scholarly literature, articles, and models related to methodology integration. After data collection, the literature is analyzed for recurring themes such as cultural challenges, documentation gaps, planning conflicts, and the need for structured transition strategies.

The study then synthesizes these findings to design a **hybrid model** inspired by the Agile Research Network collaboration model shown in the provided document. The enhanced model integrates Waterfall's upfront planning with Agile's iterative execution. This allows

for reduced development time, smoother transition phases, and better stakeholder communication.

The final outcome is a conceptual hybrid framework supported by literature evidence and comparative analysis.

2. Data Collection

The data for this research is entirely drawn from **secondary sources**, focusing on published studies, conference papers, and documented project management models.

2.1 Literature-Based Data Collection

=Data was collected from peer-reviewed research publications that discuss:

- Waterfall methodology history, structure, and challenges
- Agile methodology principles, processes, and limitations
- Hybrid models such as Water-Scrum-Fall
- Transition strategies including communication, training, and iterative pilots
- Case studies involving mixed-method projects

The provided PDF includes references from authors such as Kuhrmann et al. (2017), Barroca et al. (2018), Mohamed (2016), and Nguyen & Dupuis (2019), all of whom contribute important insights about real-world implementation challenges and hybrid practices.

2.2 Document Analysis

The research also analyzes models and visuals presented in the uploaded document:

- The **Agile Research Network Collaboration Model**, showing a 12-week cycle.
- The **Enhanced Hybrid Model**, showing reduced project duration using Waterfall–Agile integration.

By comparing these models, the research identifies measurable improvements and supports the need for hybridization.

3. Research Techniques and Analytical Approach

This study uses the following analytical techniques:

3.1 Comparative Methodology Analysis

The research compares Waterfall and Agile based on:

- Documentation requirements
- Team culture and collaboration
- Planning and scheduling styles
- Adaptability to changing requirements
- Risk and quality management

These comparisons help highlight the gaps that hybrid methods aim to resolve.

3.2 Model Evaluation and Synthesis

Using the diagrams from the provided document, the research evaluates:

- Time taken in traditional Agile model (12+ weeks)
 - Time taken in proposed hybrid model (4 weeks)
- The analysis helps validate the efficiency of integration.

This evaluation supports the creation of a structured hybrid approach.

Agile and Waterfall methodologies:

Agile and Waterfall methodologies It can be observed that the waterfall methodology was first introduced in 1970 by Royce and it is often regarded as the traditional approach to the software development process. Furthermore, this methodology follows a linear and sequential process and focuses on detailed documentation and extensive planning. Furthermore, Agile methodologies like Extreme Programming and Scrum are focusing on prioritizing collaboration, development.

flexibility, and iterative Another author discussed some challenges in the transition of these methodologies in detail. From this, the first challenge is related to cultural shift. This challenge is involved in transitioning between Agile and Waterfall methodologies. Due to this fact, the organization often need to shift from the current organizational culture to one that values self-organization and collaboration between the employees.

The second challenge is related to documentation. The facts show that there is a huge contrast present in documentation requirements between Agile and Waterfall methodologies. Therefore, the researcher provided valuable information on the focus of Agile on working software over the documentation process. It has had a huge impact on governance and project management of the project.

The third challenge is related to change management and it is a recurring theme in the literature. The main focus of the research is on the need for change management strategies to facilitate the transition process effectively. The last challenge was related to project planning and there were some important challenges present related to plan project planning with Waterfall and Agile methodology. It was not simple to maintain a balance between adaptive planning and upfront planning by using these methodologies.

Bridging the Gap: Strategies and Approaches

There are a lot of authors who have provided some valuable information regarding bridging the gap between Agile and Waterfall methodologies.

The first strategy is related to hybrid models. The author described that by combining elements of these methodologies, it is possible to gain popularity. According to this, if the water-scrum-fall model is integrated with the waterfall's upfront planning with the Agile development and testing process, then positive results will be obtained for the project.

The second strategy is related to training and education for staff members. The researchers are suggesting that investing in training and education is extremely important for the successful transition of these methodologies. The working teams must understand the principles and practices of both methodologies.

The third strategy is related to clear communication. For the transiting process, there is a need for clear communication channels. Therefore, it is possible to manage expectations and ensure all stakeholders understand the project's progress, deliverables, and changes.

Another strategy is related to iterative transition. For this, an iterative approach will be used to transition the process for both methodologies. Due to this, the organization can start the process with a small-scale pilot project for testing the waters and gathering valuable insights about the project.

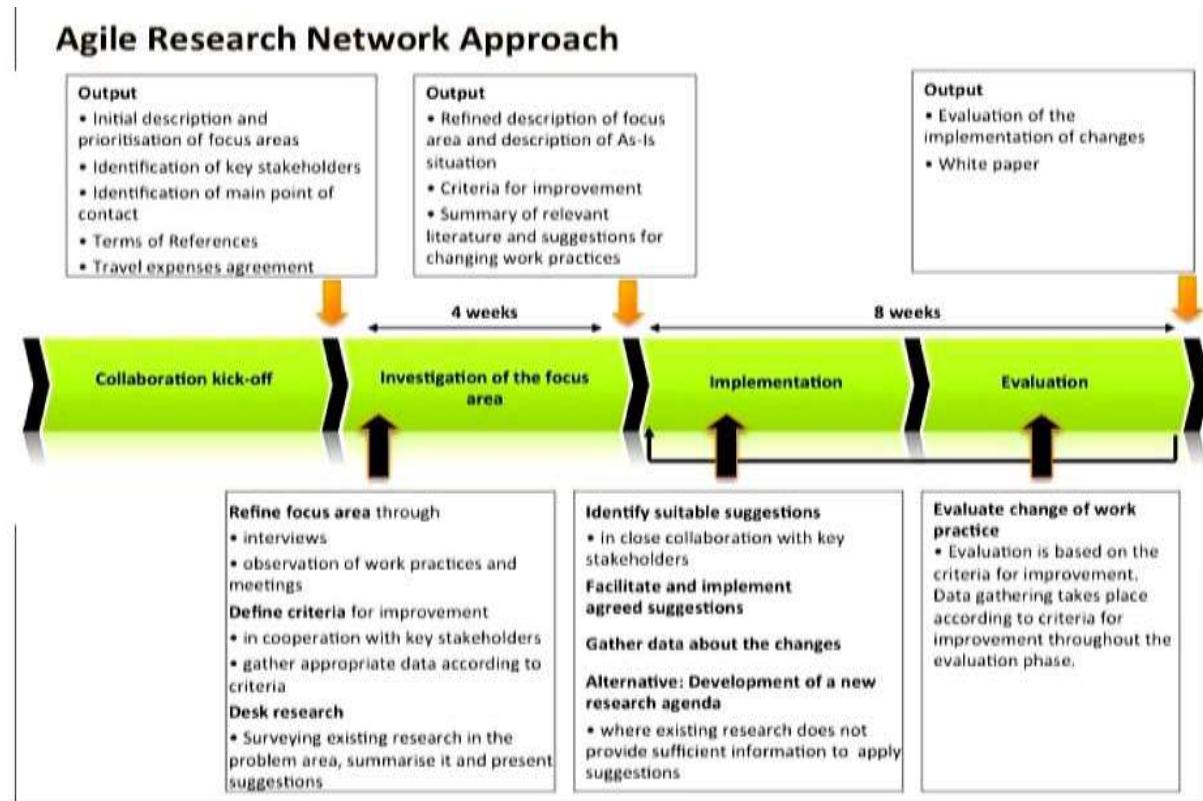


Figure 1: The complete information about the Agile Research Network Collaboration Model

The above image shows information about the Agile methodology research network collaboration network. This network consists of various phases. Also, in every phase, there is proper time to complete it with ease. The collaboration kick-off phase is extremely important because it will elaborate and define all phases in detail and also show important results. Secondly, the investigation of the focus area will take about 4 weeks of this process. After this, in the implementation phase and evaluation phase, the software will be tested and implemented properly. It shows that the required phase is taking a lot of time about 8 weeks. Under these facts, there is a need to fill the gap by transiting Waterfall and Agile methodologies.

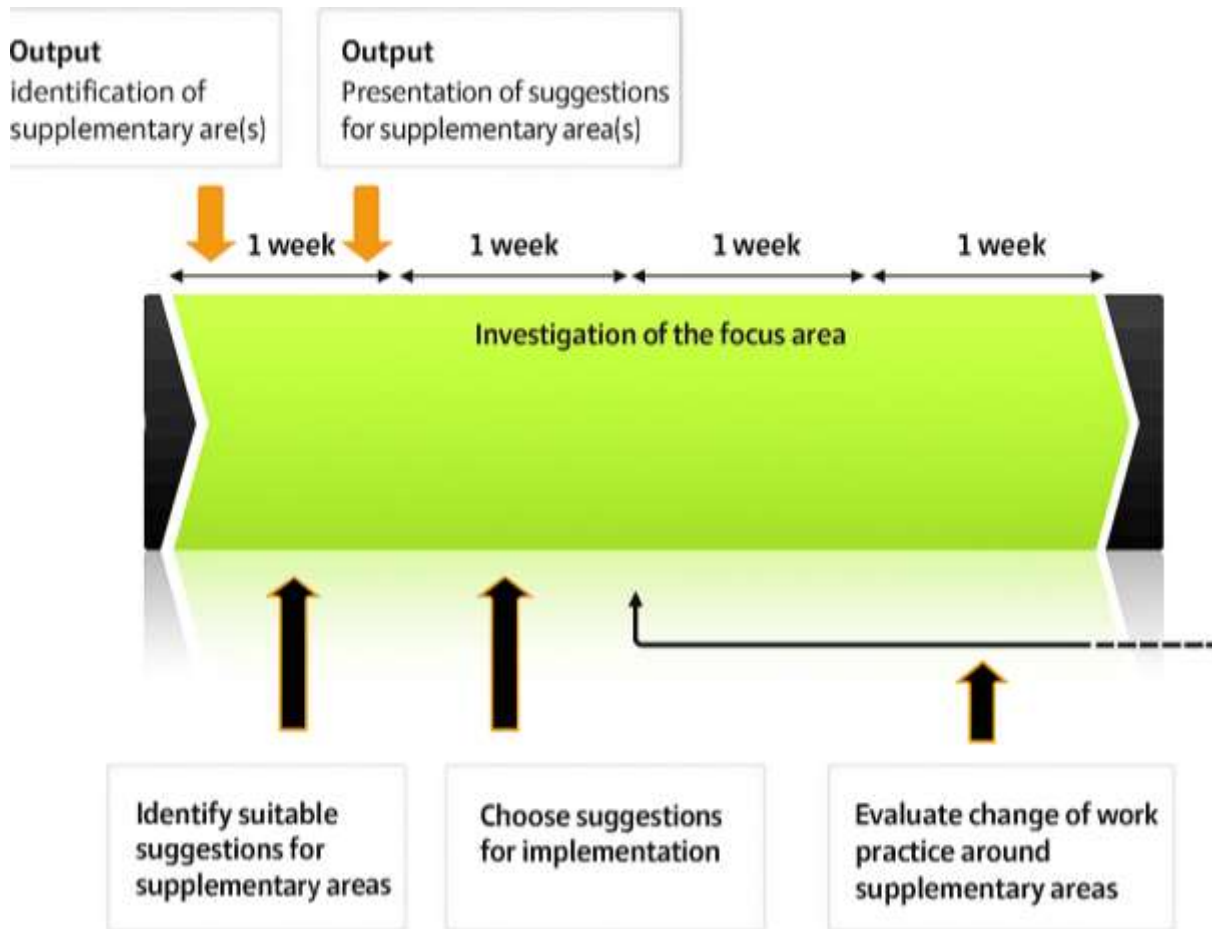


Figure 2: An enhanced Agile Research Network approach collaboration model with all processes

The above image shows valuable information after applying the transition of Waterfall and Agile methodology. According to this, these results show that positive outcomes are obtained in the software development process by combining these methodologies in detail. The whole process will be completed within 4 weeks. However, the above Agile research collaboration model took more than 12 weeks to complete. Therefore, it is not very valuable for software development applications.

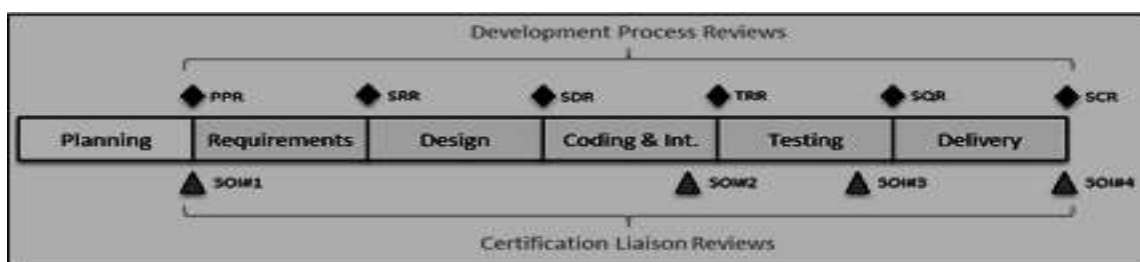


Figure 3: Software Development Lifecycle for DO-178C

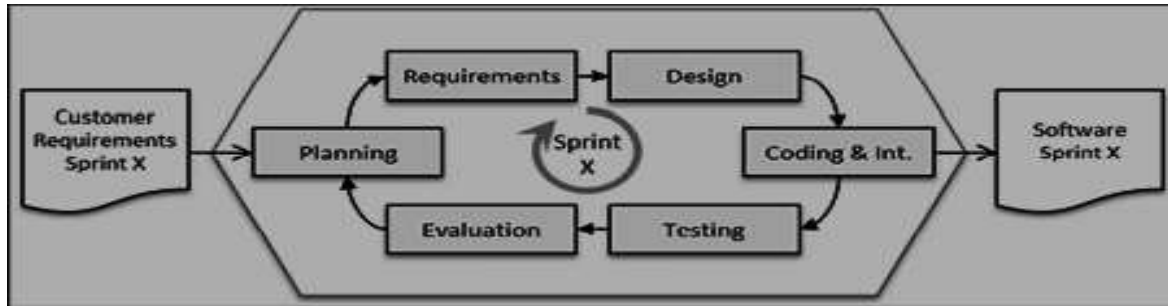


Figure 4: Agile Software Development Lifecycle

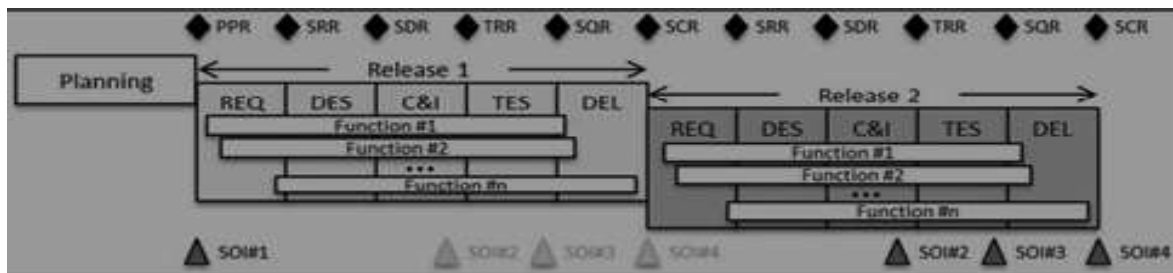


Figure 6: Functional Process of the software

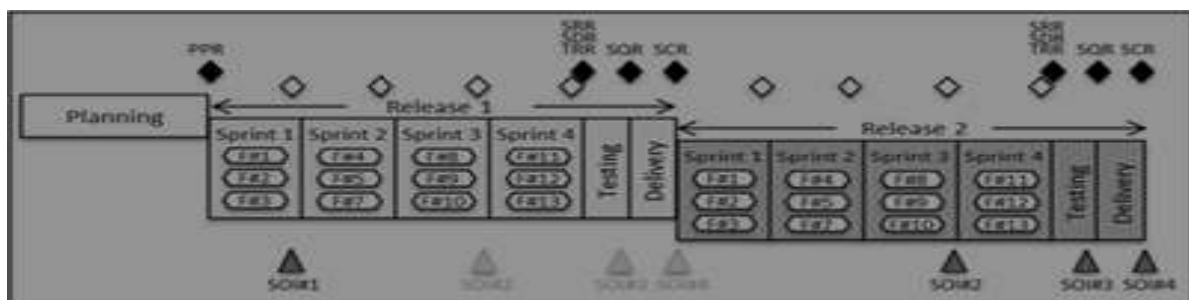


Figure 7: Agile process for the software

The four images collectively illustrate how software development can transition from the traditional **Waterfall model** to modern **Agile practices**. In all the diagrams, the core phases of the software development lifecycle remain consistent: **planning, requirements, design, coding, testing**, and finally **delivery** of the software product.

Figure 4 highlights that while Agile enables a **faster and iterative development cycle**, it also introduces certain challenges such as frequent requirement changes, continuous customer involvement, and the need for high team coordination.

The remaining figures demonstrate how the transition between **Waterfall and Agile methodologies** can be managed by adopting intermediate or hybrid strategies:

- The **Incremental Process** breaks the system into smaller parts, allowing portions of the software to be developed and delivered step-by-step.
- The **Functional Process** organizes development around functional modules, each going through its own mini-lifecycle of requirements, design, coding, and testing.
- The **Agile Process** refines this further by using short, repeated sprints to deliver continuous improvements.

Together, these approaches show that combining incremental development, functional modelling, and Agile principles makes it easier to enhance the software development process. This hybrid strategy maintains structure (from Waterfall) while gaining flexibility and speed (from Agile), resulting in a more efficient and higher-quality development lifecycle.

Expected Outcomes & Innovation:

Key results expected from the research or project:

- **Understanding Challenges and Opportunities:** The research aims to provide a clear understanding of the challenges and opportunities involved in integrating Waterfall and Agile methodologies in software development.
- **Practical Hybrid Strategies:** It seeks to offer practical strategies for organizations to effectively implement a hybrid approach that combines elements of both methodologies.
- **Demonstrated Time Savings:** The project is expected to demonstrate the potential for significant time savings in software development projects, as illustrated by the comparison between Figure 1 (Agile Research Network Collaboration Model) and Figure 2 (Enhanced Agile Research Network approach collaboration model).
- **Improved Project Outcomes:** The ultimate goal is to show how adopting these strategies can lead to enhanced project adaptability, improved project outcomes, and increased market competitiveness for organizations.

Academic Contribution:

- **Knowledge Synthesis:** The research provides a valuable summary of existing knowledge regarding Waterfall and Agile methodologies and their integration.

- **Framework Proposal:** It proposes a framework for effective methodology integration, contributing to the academic discourse on software development project management.

Industrial Contribution:

- **Practical Guidance:** The project offers useful tips and strategies for project managers and organizations.
- **Process Improvement:** It aims to help industries improve their software development processes.
- **Enhanced Results:** The research provides insights for achieving better results in the dynamic and evolving software development environment.

Comparative Analysis

Parameter	Waterfall Model	Agile Model	Hybrid Model (Waterfall + Agile)
Development Style	Linear and sequential	Iterative and incremental	Combination of sequential and iterative
Requirement Handling	Fixed at beginning	Evolving requirements	Initially fixed, refined iteratively
Planning Approach	Extensive upfront planning	Adaptive planning	Upfront + iterative planning
Documentation	Heavy documentation	Minimal documentation	Balanced documentation
Customer Involvement	Limited	Continuous	Periodic and continuous
Flexibility to Change	Very low	Very high	Medium to high
Risk Management	High risk with changes	Lower risk	Optimized risk handling
Development Speed	Slow	Fast	Moderate to fast

Testing Phase	After development	Continuous testing	Continuous testing after planning
Team Structure	Hierarchical	Self-organizing teams	Structured yet collaborative
Cost Predictability	High	Low	Moderate
Project Suitability	Stable & regulated projects	Dynamic projects	Large & complex projects
Main Advantage	Clear structure	High adaptability	Stability + flexibility
Main Limitation	Rigid to change	Low predictability	Requires coordination

Conclusion

Summing up all the discussion from above, it is concluded that in the changing software development landscape, there is a need for proper adaption, and finding the right balance between the two methodologies Agile and Waterfall is extremely important. However, the transition between these two methodologies is extremely challenging. If the right and accurate strategies are implemented, then organizations can easily bridge the gap between these methodologies effectively. Furthermore, by leveraging the strengths of both methodologies in detail and addressing the associated challenges, organizations can enhance their adaptability, remain competitive in the market, and improve project outcomes. For the software development process, there are a lot of phases for its development. By making an accurate bridge, successful results can be obtained.

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AI-Based Data Analytics: Opportunities and Challenges

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Abstract:

The rapid growth of data generated from digital platforms, organizations, and connected systems has increased the demand for advanced analytical techniques. Traditional data analytics methods often struggle to handle large volumes of complex and unstructured data effectively. Artificial Intelligence (AI) has emerged as a powerful approach to enhance data analytics by enabling automated learning, pattern recognition, and predictive insights. This research paper examines the role of AI-based data analytics, focusing on its key opportunities and challenges.

The study highlights how AI techniques such as machine learning and deep learning improve decision-making, accuracy, and efficiency across various application domains including business intelligence, healthcare, and finance. At the same time, the paper discusses major challenges associated with AI-driven analytics, such as data quality issues, ethical concerns, lack of transparency, high computational requirements, and skill gaps.

By analyzing existing literature and real-world use cases, this paper provides a balanced understanding of the potential and limitations of AI-based data analytics. The study concludes that while AI significantly enhances analytical capabilities, addressing its challenges is essential for sustainable and responsible adoption.

Keywords: Artificial Intelligence, AI-Based Analytics, Machine Learning Algorithms, Big Data Analytics, Data-Driven Decision Making, Ethical Challenges

INTRODUCTION

The rapid growth of digital technologies has led to the generation of massive amounts of data, creating new challenges for traditional data analytics methods. Conventional analytical techniques often fail to effectively process large and complex datasets, increasing the need for advanced analytical approaches. Artificial Intelligence (AI) has emerged as a powerful solution by enabling automated data analysis, pattern recognition, and predictive insights.

AI-based data analytics uses techniques such as machine learning and deep learning to improve accuracy and support data-driven decision making across various domains including business, healthcare, and finance.

REVIEW OF LITERATURE

AI Techniques in Data Analytics

Smith and Johnson (2019) explained that Artificial Intelligence techniques such as machine learning, deep learning, and neural networks have significantly transformed traditional data analytics by enabling automated learning from data. Their study highlighted that AI models are capable of handling high-dimensional and unstructured datasets more effectively than conventional statistical methods. Similarly, Brown et al. (2020) emphasized that AI-driven analytics systems improve prediction accuracy and scalability, making them suitable for big data environments. The authors also noted that continuous learning capabilities of AI models allow organizations to adapt to changing data patterns over time.

Application of AI-based Data Analytics

The application of AI-based data analytics has been widely discussed in existing literature. Miller and Davis (2021) reported that organizations increasingly use AI-driven analytics in business intelligence to support strategic planning, customer behavior analysis, and demand forecasting. In the healthcare domain, Kumar and Patel (2020) demonstrated that AI-based analytics assists in early disease detection, medical image analysis, and personalized treatment planning. Furthermore, Lee et al. (2019) examined the role of AI analytics in the financial sector and found that AI techniques significantly improve fraud detection, risk assessment, and financial forecasting accuracy. These studies collectively highlight the versatility and effectiveness of AI-based data analytics across multiple industries.

Challenges Related to AI-Based Data Analytics

Despite its advantages, several studies have identified major challenges associated with AI-based data analytics. Wilson and Clarke (2020) stated that poor data quality, including incomplete and biased datasets, negatively affects the reliability of AI models. Anderson (2021) discussed ethical concerns related to data privacy, surveillance, and misuse of personal data in AI-driven analytics systems. Additionally, Zhang et al. (2019) pointed out

that the lack of transparency and interpretability in complex AI models creates trust issues among users and decision-makers. These challenges highlight the need for responsible and transparent AI implementation in analytics.

Limitations and Research Gaps in Existing Studies

Several researchers have also addressed the practical limitations of AI-based data analytics systems. Roberts and Green (2021) highlighted that high computational costs and advanced infrastructure requirements limit the adoption of AI analytics, especially for small and medium-sized organizations. Fernandez et al. (2020) emphasized the shortage of skilled professionals capable of designing, implementing, and maintaining AI-based analytical systems

RESEARCH GAP

Despite the growing body of research on AI-based data analytics, several gaps remain that justify further study. Most existing studies focus either on the applications or the technical advantages of AI techniques in analytics, such as improved accuracy, predictive modeling, and automation. For instance, studies by Miller and Davis (2021) and Kumar and Patel (2020) extensively discuss industry applications but provide limited insights into the combined evaluation of opportunities and challenges.

Similarly, while some researchers, including Wilson and Clarke (2020) and Anderson (2021), highlight challenges such as data quality, ethical issues, and model transparency, there is insufficient research integrating these challenges with practical opportunities across multiple sectors. Furthermore, practical limitations such as high computational costs, infrastructure requirements, and skill gaps are mentioned separately but rarely analyzed alongside the benefits in a holistic framework (Roberts & Green, 2021; Fernandez et al., 2020).

This lack of an integrated perspective limits the understanding of how AI-based analytics can be implemented effectively while mitigating risks. Therefore, there is a clear need for research that examines both the opportunities and challenges of AI-based data analytics simultaneously, providing actionable insights for organizations planning to adopt AI-driven analytics systems. This study addresses this gap by offering a balanced analysis of the benefits, limitations, and practical implications of AI-based data analytics.

OBJECTIVES OF THE RESEARCH

Primary Object

The primary objective of this study is to examine the opportunities and challenges associated with AI-based data analytics. The research aims to provide a clear understanding of how AI techniques, such as machine learning and deep learning, enhance data-driven decision-making processes while addressing the limitations and risks inherent in AI-driven systems.

Exploring Opportunities

A key objective is to explore the significant opportunities offered by AI-based data analytics. This includes improved predictive accuracy, automation of complex data analysis tasks, real-time decision-making support, and enhanced operational efficiency. The study will also examine how AI applications benefit multiple domains, including business intelligence, healthcare, and finance.

Identifying Challenges

Another important objective is to identify and analyze the major challenges and limitations associated with AI-based analytics. The study focuses on issues such as data quality, ethical concerns, lack of transparency, high computational requirements.

Practical Applications and Recommendations

This research also aims to analyze real-world applications and case studies of AI-based data analytics to understand the practical benefits and constraints of its implementation. Based on these insights, the study will provide recommendations for organizations seeking to adopt AI-driven analytics, ensuring they can maximize opportunities while mitigating potential risks.

RESEARCH METHODOLOGY

The study is descriptive and analytical in nature. It focuses on analyzing the opportunities and challenges of AI-based data analytics across multiple sectors.

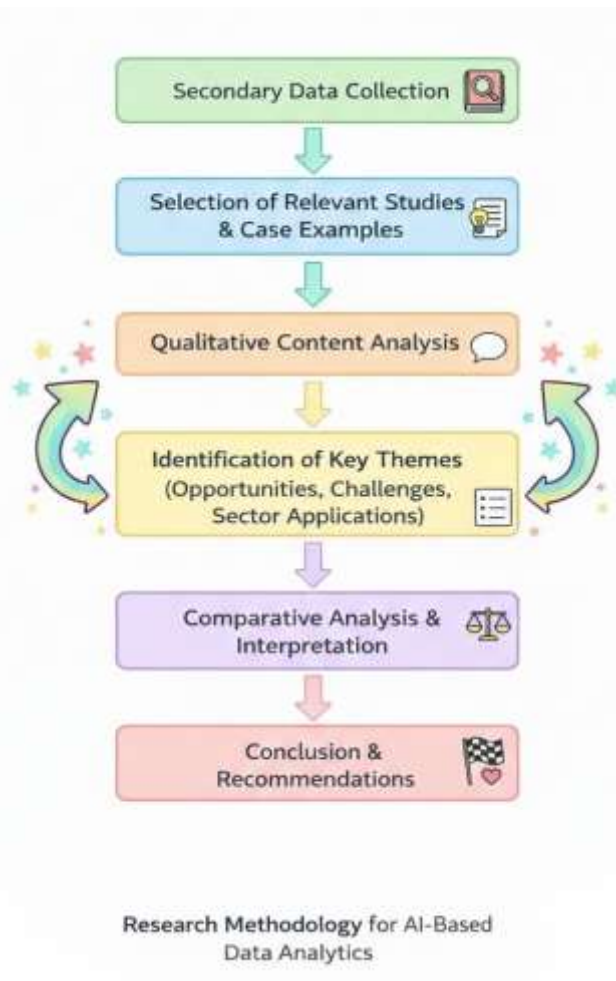


Figure 2: Research Methodology Framework

1. Data Collection:

The study uses **secondary data sources**:

- Research articles
- Industry reports
- Authoritative websites and databases

The data is carefully selected based on:

- **Relevance:** Only studies related to AI in analytics are considered.
- **Credibility:** Only trustworthy, published sources are included.
- **Recency:** Latest studies are prioritized to reflect current trends.

2. Sampling:

The research reviews selected case studies and articles related to AI applications in business, healthcare, and finance. These are chosen to cover diverse sectors and provide a broad understanding of opportunities and challenges.

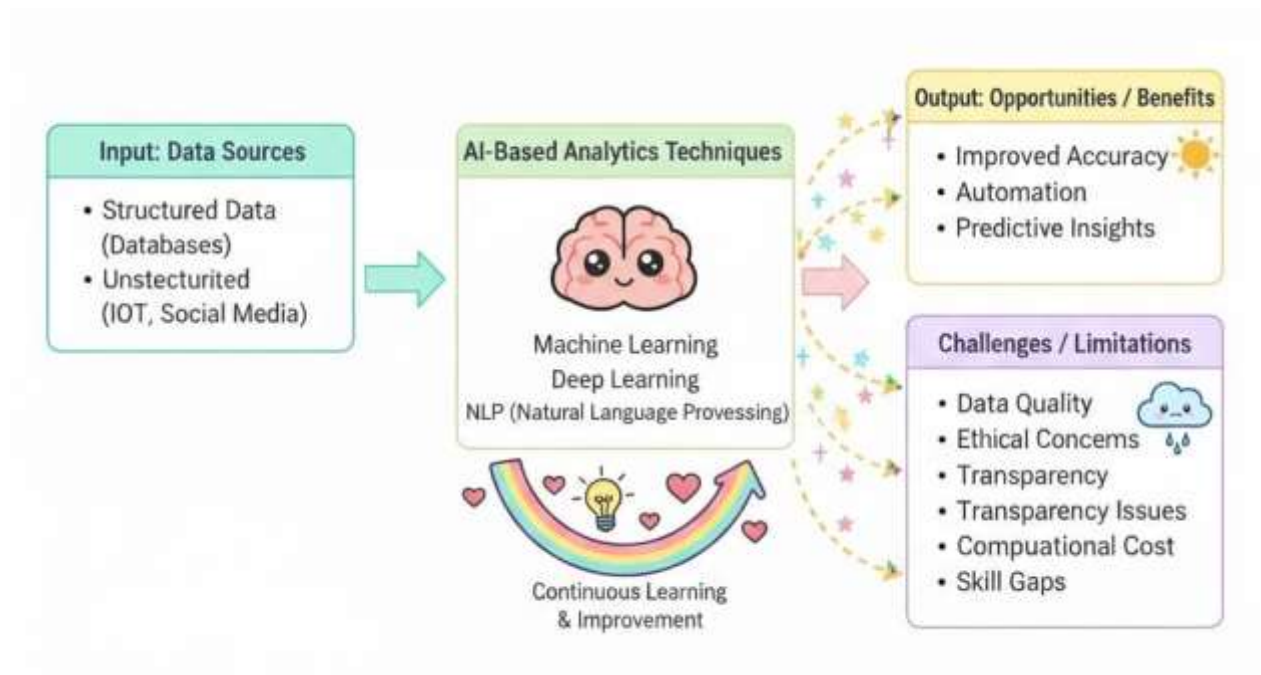
3. Data Analysis Techniques:

The study employs a **qualitative content analysis** approach to examine the collected literature. Key themes are extracted from the literature, including the opportunities offered by AI-based analytics, such as improved accuracy, automation of tasks, and predictive insights; the challenges faced, including issues related to data quality, ethical concerns, model transparency, and implementation costs; and sector-specific applications across business, healthcare, and finance. Additionally, a comparative approach is used to highlight differences and similarities across sectors, providing a clear and organized summary of the findings.

4. Scopes and Limitations:

The scope of this study focuses on the applications and challenges of AI-based data analytics in organizational and industrial contexts. It examines the opportunities, limitations, and potential directions for future research in AI analytics. However, the study has certain limitations. It relies solely on secondary data, which means it may not fully reflect proprietary practices or the most recent developments in AI analytics. Furthermore, no primary data collection through surveys or experiments is conducted. Despite these limitations, the study provides a comprehensive and balanced overview of AI-based data analytics, highlighting both its potential and the challenges that need to be addressed for effective implementation.

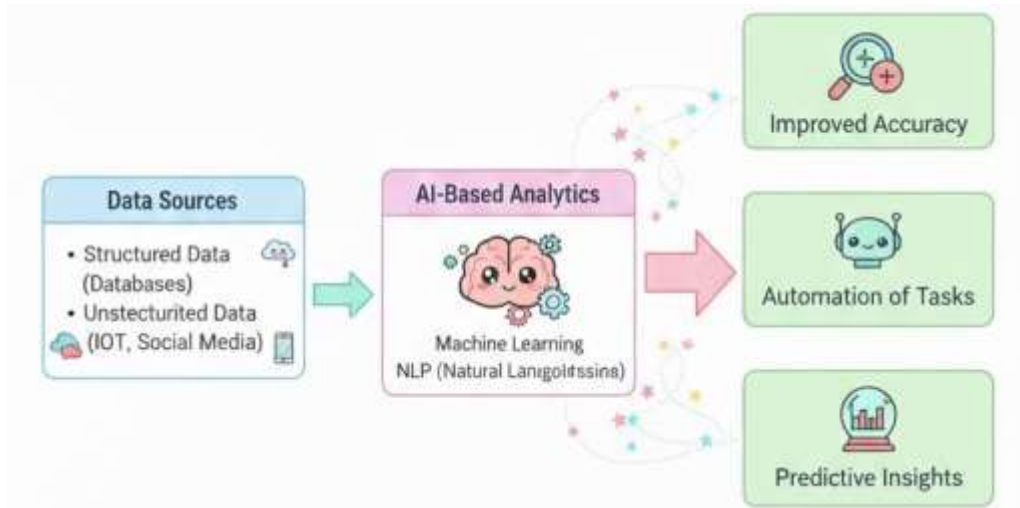
Model Diagram:-



RESULTS AND DISCUSSION

1. Opportunities in AI- Based Data Analytics:

The analysis of existing literature and case studies reveals that AI-based data analytics offers substantial opportunities across various domains. In business, AI-driven analytics improves decision-making by providing accurate predictive insights, automating routine tasks, and optimizing operations (Miller & Davis, 2021). In healthcare, AI enhances diagnostic accuracy and supports personalized treatment planning (Kumar & Patel, 2020). Financial institutions benefit from AI-based fraud detection, risk assessment, and portfolio management (Lee et al., 2019). These findings demonstrate that AI significantly increases efficiency, accuracy, and speed in data-driven decision-making.



Opportunities for AI-Based Data Analysis

2. Sector Specific Observations:

Comparative analysis across sectors highlights both shared and sector-specific patterns. Business applications predominantly focus on predictive marketing, operational optimization, and customer analytics. Healthcare applications emphasize patient diagnostics, treatment planning, and medical image analysis. In finance, AI is widely applied in risk management, fraud detection, and investment decision-making. While the core AI techniques—such as machine learning and deep learning—are similar across sectors, the application priorities differ, showing the need for customized AI solutions for each sector.

3. Implications:

The findings suggest that AI-based analytics can significantly enhance organizational performance if implemented strategically. Organizations should prioritize data quality improvement, invest in skilled personnel, and ensure ethical and transparent AI practices. Policymakers and researchers can leverage these insights to develop frameworks for responsible AI adoption, while future studies can focus on improving interpretability, scalability, and sector-specific customization of AI analytics solutions.

CONCLUSION

Artificial Intelligence (AI) has emerged as a transformative tool in the field of data analytics, offering significant opportunities for organizations across various sectors. This study highlights that AI-based analytics enhances predictive accuracy, automates complex tasks,

and enables real-time decision-making, particularly in business, healthcare, and finance. These benefits demonstrate the potential of AI to improve operational efficiency and support strategic planning.

However, the research also identifies notable challenges that organizations must address for effective implementation. Data quality issues, ethical concerns, lack of transparency, high computational costs, and the shortage of skilled professionals remain significant barriers. A balanced approach is essential to maximize opportunities while mitigating risks.

The findings of this study suggest that AI-based data analytics can significantly improve organizational performance when implemented strategically with attention to data governance, ethical practices, and workforce readiness. Organizations should focus on integrating AI tools responsibly, customizing solutions for sector-specific requirements, and continually monitoring AI models to ensure reliability and accountability.

FUTURE SCOPE

The field of AI-based data analytics holds significant potential for further development and research. Future studies can focus on enhancing the transparency and interpretability of AI models, which will help organizations build trust in AI-driven decisions. Research can also explore strategies for improving data quality management, ethical compliance, and privacy protection, addressing the challenges identified in this study.

Another important area is the application of AI analytics in emerging sectors and small-to-medium enterprises, where adoption is currently limited due to infrastructure and skill constraints. Developing sector-specific frameworks and scalable solutions can facilitate effective AI integration tailored to organizational needs.

Moreover, advances in explainable AI (XAI), adaptive learning algorithms, and hybrid analytics models offer opportunities for more efficient, reliable, and responsible use of AI in large-scale data analysis. Policymakers and organizations can leverage these insights to implement AI-based analytics systems that maximize benefits while minimizing risks, ensuring sustainable growth and innovation.

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A Study on Cloud Computing: Architecture, Services, and Applications

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Abstract: Cloud computing is one of the most important technologies in the modern information technology era. It provides computing resources such as storage, servers, applications, and software through the internet instead of local systems. Cloud computing reduces the need for physical infrastructure and allows users to access data anytime and from anywhere. This research paper explains the basic concept of cloud computing, its architecture, service models, deployment models, advantages, challenges, and real-world applications. The paper also discusses security issues and the future scope of cloud computing. With the rapid growth of digital services, cloud computing has become an essential part of business, education, healthcare, and government sectors. This study aims to give a clear and easy understanding of cloud computing for beginners and students.

Keywords: Cloud Computing, IaaS, PaaS, SaaS, Virtualization, Data Security

1. INTRODUCTION

In the present digital era, information technology has become an essential part of daily life. With the rapid growth of the internet and digital services, the need for efficient data storage, processing, and management has increased significantly. Traditional computing systems depend on local servers and physical infrastructure, which are costly to maintain and difficult to scale. To overcome these limitations, cloud computing has emerged as a powerful and flexible computing model.

Cloud computing is a technology that allows users to access computing resources such as storage, servers, software, databases, and networking services through the internet. Instead of installing software or maintaining hardware on personal computers, users can simply use cloud-based services provided by third-party vendors. These services are available on demand and can be accessed from anywhere at any time using an internet connection. This makes cloud computing highly convenient and cost-effective for both individuals and organizations.

One of the main reasons for the popularity of cloud computing is its ability to reduce operational costs. Organizations do not need to invest heavily in hardware, software licenses, or maintenance staff. Cloud service providers handle infrastructure management, updates, security, and backups. Users only pay for the services they use, which makes cloud computing suitable for small, medium, and large enterprises.

Cloud computing also offers high scalability and flexibility. Resources can be increased or decreased according to user requirements. This feature is especially useful for businesses that experience fluctuating workloads. In addition, cloud computing supports collaboration by allowing multiple users to work on the same data or application simultaneously.

Today, cloud computing is widely used in various sectors such as education, healthcare, banking, business, and government services. Technologies like artificial intelligence, big data, and the Internet of Things are further increasing the importance of cloud computing. Due to its wide range of applications and benefits, cloud computing has become a core component of modern information technology systems.

2. EVOLUTION OF CLOUD COMPUTING

The concept of cloud computing did not appear suddenly; it evolved gradually from earlier computing technologies. The idea of sharing computing resources can be traced back to the 1960s when mainframe computers were used by multiple users through terminals. During this time, computing resources were expensive, and sharing them was considered an efficient solution.

In the 1970s and 1980s, the development of time-sharing systems and distributed computing further strengthened the concept of shared resources. Multiple computers were connected through networks to work together and share processing power. However, these systems were complex and difficult to manage.

In the 1990s, the growth of the internet played a major role in the evolution of cloud computing. Technologies such as client-server architecture and web-based applications became popular. Organizations started hosting applications on centralized servers that could be accessed through web browsers. This period also saw the emergence of Application

Service Providers (ASPs), which offered software services over the internet, similar to today's SaaS model.

The early 2000s marked a major turning point with the introduction of virtualization technology. Virtualization made it possible to run multiple virtual machines on a single physical server, improving hardware utilization and reducing costs. Companies like Amazon realized the potential of this technology and launched cloud services such as Amazon Web Services (AWS) in 2006.

Later, major technology companies like Google and Microsoft introduced their own cloud platforms, including Google Cloud Platform and Microsoft Azure. These platforms offered scalable infrastructure, platforms, and software services to users worldwide.

Today, cloud computing has become a mature and widely adopted technology. It supports advanced technologies such as artificial intelligence, big data analytics, and the Internet of Things. The continuous evolution of cloud computing is shaping the future of information technology and digital services.

3. CLOUD COMPUTING ARCHITECTURE

Cloud computing architecture refers to the overall design and structure that enables the delivery of cloud services to users through the internet. It defines how various hardware and software components are organized and interact with each other to provide scalable, reliable, and on-demand computing services. A proper cloud architecture ensures efficient resource utilization, high availability, data security, and smooth performance. The architecture of cloud computing is mainly divided into the front end and the back end, which are connected through a network, usually the internet.

The **front end** represents the user side of cloud computing. It includes client devices such as desktops, laptops, smartphones, tablets, and web browsers. Through the front end, users can access cloud services, upload or download data, run applications, and manage their accounts. The front-end interface is designed to be simple and user-friendly so that users do not need deep technical knowledge to use cloud services. Web-based dashboards and applications act as the main interface between users and the cloud.

The **back end** forms the core of cloud computing architecture and is managed by cloud service providers. It consists of physical servers, virtual machines, storage systems, databases, and application servers located in large data centers. The back end is responsible for processing user requests, storing data securely, and delivering services efficiently. It also includes management software that monitors performance, manages workloads, and ensures fault tolerance.

A key component of cloud architecture is **virtualization**. Virtualization technology allows multiple virtual machines to run on a single physical server. Each virtual machine operates independently with its own operating system and applications. This improves hardware utilization, reduces operational costs, and allows quick scaling of resources based on demand.

Middleware acts as a communication layer between the front end and the back end. It manages data exchange, authentication, and coordination between different services. The **network infrastructure**, including the internet, routers, switches, and firewalls, connects users to cloud data centers and ensures secure and fast data transfer. Overall, cloud computing architecture provides a strong foundation for delivering flexible, scalable, and secure computing services.

4. CLOUD SERVICE MODELS

Cloud computing provides services to users through different service models. These models define the level of control, flexibility, and responsibility shared between the cloud service provider and the user. The three main cloud service models are Infrastructure as a Service (IaaS), Platform as a Service (PaaS), and Software as a Service (SaaS). Each model is designed to meet different user and business requirements.

4.1 Infrastructure as a Service (IaaS)

Infrastructure as a Service is the basic service model of cloud computing. In IaaS, cloud service providers offer virtualized computing resources such as servers, storage, networking, and virtual machines over the internet. Users do not need to purchase or maintain physical hardware. They have control over operating systems, storage, and applications, while the cloud provider manages the physical infrastructure. IaaS is mainly used by organizations that require high flexibility and control over their computing environment. Common examples of

IaaS include Amazon Elastic Compute Cloud (EC2), Microsoft Azure Virtual Machines, and Google Compute Engine.

4.2 Platform as a Service (PaaS)

Platform as a Service provides a complete development and deployment environment in the cloud. PaaS allows developers to build, test, and deploy applications without worrying about underlying hardware or system software. The cloud provider manages servers, storage, networking, operating systems, and runtime environments, while users focus only on application development. PaaS increases developer productivity and reduces development time. It is widely used for web and mobile application development. Popular examples of PaaS include Google App Engine, Microsoft Azure App Services, and Heroku.

4.3 Software as a Service (SaaS)

Software as a Service is the most widely used cloud service model. In SaaS, software applications are delivered to users over the internet on a subscription or free basis. Users can access applications through web browsers without installing or maintaining software on their local systems. The cloud provider handles application management, updates, security, and maintenance. SaaS is commonly used for email services, document editing, customer relationship management, and collaboration tools. Examples of SaaS include Gmail, Google Docs, Microsoft Office 365, and Salesforce.

In summary, cloud service models provide different levels of services to meet diverse user needs. Organizations can choose the most suitable model based on cost, control, scalability, and application requirements.

5. CLOUD DEPLOYMENT MODELS

Cloud deployment models define how cloud infrastructure is set up, owned, and accessed. They help organizations choose the right cloud environment based on security needs, cost, scalability, and control. The four main cloud deployment models are **Public Cloud, Private Cloud, Hybrid Cloud, and Community Cloud**.

1. Public Cloud

The **public cloud** is owned and managed by third-party cloud service providers such as Amazon Web Services (AWS), Microsoft Azure, and Google Cloud Platform (GCP). In this model, computing resources like servers, storage, and applications are shared among multiple users over the internet.

Public cloud services are usually provided on a **pay-as-you-use** basis, making them cost-effective for startups, students, and small to medium-sized businesses. It offers high scalability, easy maintenance, and global accessibility. However, since resources are shared, organizations may have less control over data security and compliance compared to private environments.

Key Features:

- Shared infrastructure
- Low initial cost
- High scalability and availability
- Managed by third-party providers

2. Private Cloud

A **private cloud** is dedicated to a single organization. It can be hosted either on-premises or by a third-party provider, but the infrastructure is used exclusively by one organization. This model offers greater control over data, security, and compliance.

Private clouds are ideal for large enterprises, government organizations, and institutions handling sensitive data. Although more secure and customizable, private clouds require higher investment and maintenance costs compared to public clouds.

Key Features:

- Exclusive use by one organization
- High security and privacy
- Greater control and customization
- Higher cost and management effort

3. Hybrid Cloud

The **hybrid cloud** combines both public and private cloud models. It allows data and applications to be shared between them, offering greater flexibility. Organizations can keep sensitive data in a private cloud while using the public cloud for less critical operations or to handle workload spikes.

This model helps optimize cost and performance while maintaining security. Hybrid clouds are widely used in businesses that need scalability along with data protection.

Key Features:

- Combination of public and private clouds
- Flexible workload management
- Better cost optimization
- Enhanced security for sensitive data

4. Community Cloud

A **community cloud** is shared by several organizations with similar requirements, such as security, compliance, or industry regulations. Examples include cloud infrastructures used by universities, healthcare institutions, or government departments.

The cost is shared among participating organizations, making it more affordable than a private cloud while offering better security than a public cloud. Management can be handled by one or more organizations or a third party.

Key Features:

- Shared by organizations with common goals
- Cost-effective compared to private cloud
- Supports compliance and collaboration
- Limited scalability compared to public cloud

6. APPLICATIONS OF CLOUD COMPUTING

Cloud computing is widely used across different industries due to its flexibility, scalability, cost-effectiveness, and easy accessibility. It allows users to store data, run applications, and access services over the internet without managing physical hardware. Below are the major applications of cloud computing explained in detail.

1. Data Storage and Backup

One of the most common applications of cloud computing is **data storage and backup**. Cloud platforms provide secure storage for files, databases, and multimedia content. Organizations can store large volumes of data and access it from anywhere. Automatic backup and disaster recovery features protect data from loss due to hardware failure or cyberattacks.

Examples: Google Drive, Dropbox, Amazon S3

2. Web Hosting and Application Hosting

Cloud computing is widely used for **hosting websites and web applications**. Businesses can deploy websites without investing in physical servers. Cloud hosting offers high availability, load balancing, and scalability to handle traffic fluctuations.

Examples: AWS, Microsoft Azure, Google Cloud

3. Software as a Service (SaaS)

Cloud computing enables **SaaS applications**, where users access software through a web browser without installation. This reduces maintenance costs and ensures automatic updates.

Examples: Gmail, Microsoft 365, Salesforce, Zoom

4. Development and Testing

Developers use cloud platforms to **develop, test, and deploy applications** quickly. Cloud environments allow on-demand resources, making it easy to test applications under different conditions without purchasing hardware.

Benefits: Faster development, cost savings, easy collaboration

5. Big Data Analytics

Cloud computing supports **big data processing and analytics** by providing high computing power and storage. Organizations analyze large datasets to gain insights, improve decision-making, and predict trends.

Examples: Google BigQuery, AWS EMR, Azure Synapse

6. Artificial Intelligence and Machine Learning

Cloud platforms provide ready-to-use tools for **AI and machine learning**. These services help in image recognition, natural language processing, recommendation systems, and predictive analysis.

Examples: AWS AI Services, Google AI Platform, Azure AI

7. E-commerce and Online Services

Cloud computing powers **e-commerce platforms** by handling online transactions, inventory management, and customer data securely. It ensures scalability during peak shopping seasons.

Examples: Amazon, Flipkart, Shopify

8. Education and E-learning

In education, cloud computing supports **online learning platforms**, virtual classrooms, and digital libraries. Students and teachers can access resources anytime, anywhere.

Examples: Google Classroom, Coursera, Moodle

9. Healthcare Services

Cloud computing is used in **healthcare** for storing electronic health records (EHR), telemedicine, medical data analysis, and appointment management. It improves collaboration among healthcare professionals while ensuring data security.

10. Collaboration and Communication

Cloud-based tools enable **real-time collaboration** through document sharing, video conferencing, and team communication.

Examples: Google Docs, Microsoft Teams, Slack

7. ADVANTAGES OF CLOUD COMPUTING

Cloud computing offers numerous benefits to individuals, businesses, and organizations by providing on-demand access to computing resources over the internet. It reduces the need for physical infrastructure and enables efficient, flexible, and scalable IT operations. The major advantages of cloud computing are explained below.

1. Cost Efficiency

One of the biggest advantages of cloud computing is **cost reduction**. Users do not need to invest in expensive hardware, software, or data centers. Cloud services follow a **pay-as-you-use** model, which means organizations pay only for the resources they consume. This significantly reduces capital and maintenance costs.

2. Scalability and Flexibility

Cloud computing allows resources to be **scaled up or down** according to business needs. During high demand, additional resources can be added easily, and during low demand, they can be reduced. This flexibility helps organizations manage workloads efficiently without over-provisioning.

3. Accessibility and Mobility

Cloud services can be accessed from **anywhere and at any time** using an internet connection. This supports remote work, global collaboration, and mobile access, making cloud computing ideal for modern workplaces.

4. Automatic Updates and Maintenance

Cloud service providers handle **system updates, security patches, and maintenance** automatically. This reduces the workload on IT teams and ensures that users always have access to the latest software versions.

5. Data Backup and Disaster Recovery

Cloud platforms provide **automatic data backup and recovery solutions**, ensuring data safety in case of system failures, natural disasters, or cyberattacks. This improves business continuity and minimizes data loss.

6. High Availability and Reliability

Cloud providers use **multiple data centers** and redundancy techniques to ensure high availability. Even if one server fails, services continue running without interruption, making cloud systems highly reliable.

7. Security

Most cloud service providers implement **advanced security measures** such as encryption, access control, and continuous monitoring. While security is a shared responsibility, cloud platforms often offer better protection than traditional on-premises systems.

8. Faster Deployment

Applications and services can be **deployed quickly** in the cloud. This reduces time to market and allows businesses to innovate faster without waiting for hardware setup.

9. Environment Friendly

Cloud computing reduces the need for physical servers, leading to **lower energy consumption** and reduced carbon footprint. Efficient resource utilization makes cloud computing an environmentally friendly option.

10. Improved Collaboration

Cloud-based tools enable **real-time collaboration**, allowing multiple users to work on documents and projects simultaneously from different locations.

8. CHALLENGES AND LIMITATIONS

While cloud computing offers significant advantages, it also comes with certain **challenges and limitations** that organizations must consider before adoption. Understanding these issues is critical for effective cloud strategy and risk management.

1. Security and Privacy Issues

- Data stored on the cloud can be vulnerable to hacking, cyberattacks, or unauthorized access.
- Ensuring compliance with laws like GDPR or HIPAA is challenging.

2. Service Downtime

- Cloud services rely on internet and provider uptime.
- Outages or server failures can disrupt business operations.

3. Limited Control

- Users may have less control over infrastructure in public or hybrid clouds.
- Harder to customize systems compared to on-premises solutions.

4. Vendor Lock-in

- Moving data or apps between cloud providers is often complex and costly.
- Dependency on a single provider can limit flexibility.

5. Cost Management

- Unexpected usage spikes can increase costs.
- Continuous monitoring is needed to avoid overspending.

6. Latency and Performance

- Access speed depends on internet connectivity and distance from cloud servers.
- Real-time applications may face delays.

7. Compliance and Legal Issues

- Data may reside in multiple countries, creating legal challenges.
- Organizations must ensure providers meet industry standards.

8. Limited Customization

- Some cloud services have fixed configurations.
- Not all business-specific needs can be met easily.

9. Internet Dependency

- Cloud services cannot be accessed without a reliable internet connection.

9. CONCLUSION

Cloud computing is one of the most transformative technologies of the modern digital era. It provides **on-demand access to computing resources**—including servers, storage, databases, networking, software, and analytics—over the internet. This eliminates the need for organizations to invest heavily in physical infrastructure, making it a **cost-effective and scalable solution** for businesses of all sizes. By offering flexibility, cloud computing enables companies to **scale resources up or down** based on demand, support remote work, and improve operational efficiency.

The applications of cloud computing are vast and diverse. It supports **data storage and backup**, allowing organizations to securely store large amounts of information while enabling easy recovery in case of data loss. Cloud services also power **web hosting, software as a service (SaaS), big data analytics, artificial intelligence, and machine learning applications**, which help businesses innovate and gain actionable insights. In addition, sectors like **education, healthcare, e-commerce, and finance** leverage cloud computing to provide better services, enhance collaboration, and improve accessibility for users worldwide.

Cloud computing also brings significant **advantages**, including cost savings, faster deployment, automatic updates, high availability, enhanced collaboration, and environmental benefits due to reduced hardware usage. Organizations can focus more on core business activities rather than managing IT infrastructure. Moreover, cloud computing supports **real-time collaboration**, remote access, and global connectivity, which are essential for modern workplaces and digital transformation initiatives.

However, cloud computing is not without its challenges. **Security and privacy risks, downtime, limited control, vendor lock-in, cost management issues, latency, compliance concerns, and dependence on internet connectivity** are critical limitations that must be addressed. Organizations must implement **robust security measures, choose suitable**

deployment models (public, private, hybrid, or community), and monitor resource usage to mitigate these risks.

In conclusion, cloud computing is a **powerful and essential technology** that has reshaped the IT landscape. By providing scalable, flexible, and accessible solutions, it empowers organizations to innovate, collaborate, and grow efficiently. While challenges exist, proper planning, security, and strategic use of cloud services can maximize its benefits. As businesses and technologies continue to evolve, cloud computing will remain a **key driver of digital transformation**, supporting smarter, faster, and more efficient operations across industries worldwide.

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Effect of Nano DAP Seed Treatment on Germination and Early Growth of Wheat (*Triticum aestivum* L.)

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Abstract

Wheat (*Triticum aestivum* L.) is one of the world's most important cereal crops, and improving its early establishment is essential for achieving higher productivity. The present study entitled "Effect of Nano DAP Seed Treatment on Germination and Early Growth of Wheat (*Triticum aestivum* L.)" was conducted during the Rabi season of 2025–26 at the Agricultural Instructional Farm, School of Agricultural Sciences, Career Point University, Kota, Rajasthan. The objective was to evaluate the effect of Nano DAP seed treatment on wheat germination, seedling vigour, and early crop establishment. Healthy seeds of wheat variety Raj-4037 were divided into two treatments: T₁ (untreated control) and T₂ (Nano DAP @ 5 ml kg⁻¹ seed). After uniform coating and shade drying, the seeds were sown under identical field conditions. Observations were recorded on germination initiation, germination percentage, seedling emergence, seedling vigour, root and shoot growth, and crop establishment. The Nano DAP-treated seeds exhibited earlier germination, higher germination percentage, better seedling emergence, improved root and shoot development, and more uniform crop establishment than the untreated control. The results demonstrate that Nano DAP applied as a seed treatment enhances early plant growth and nutrient use efficiency even at a very low application rate. The study indicates that Nano DAP has considerable potential as a sustainable seed treatment technology for wheat cultivation, although long-term and multi-location studies are required to validate its effects on yield, grain quality, and soil health.

Keywords: Wheat, Nano DAP, Seed treatment, Germination, Seedling vigour.

1. Introduction

Wheat (*Triticum aestivum* L.) is one of the most important cereal crops in the world and serves as a staple food for more than one-third of the global population. In India, wheat occupies a pivotal position in the agricultural economy, contributing significantly to national food security, farmers' livelihoods, and nutritional requirements. Sustaining wheat productivity under increasing pressure from climate change, declining soil fertility, and inefficient nutrient management has become a major challenge. Therefore, the adoption of innovative nutrient management technologies is essential for achieving higher productivity while maintaining environmental sustainability (FAO, 2023; ICAR, 2024). Successful crop establishment begins with high-quality seed and efficient nutrient availability during the early stages of plant growth. Seed treatment is one of the most economical and effective agronomic practices that protects seeds against pathogens and insects while enhancing seed germination, seedling vigour, and uniform crop establishment. In recent years, seed treatment has evolved beyond the use of fungicides and insecticides to include plant growth promoters, biofertilizers, micronutrients, and nanotechnology-based fertilizers. These innovations are designed to improve nutrient use efficiency and promote healthy crop growth from the initial stages of development (Copeland and McDonald, 2001; ISTA, 2023). Among modern agricultural technologies, nanotechnology has emerged as a promising tool for improving fertilizer efficiency and reducing nutrient losses. Nanofertilizers consist of nutrients delivered in nanoparticle form or encapsulated within nanomaterials that facilitate controlled and targeted nutrient release. Compared with conventional fertilizers, nanofertilizers possess a significantly larger surface area, greater reactivity, and improved nutrient absorption efficiency. Consequently, they can supply essential nutrients in smaller quantities while minimizing losses through volatilization, leaching, and fixation in the soil. Their application is expected to increase nutrient use efficiency, improve crop productivity, reduce production costs, and lessen environmental pollution associated with excessive fertilizer application (Kah *et al.*, 2018; Dimkpa and Bindraban, 2018). Among nanofertilizers developed in India, Nano DAP (Nano Di-Ammonium Phosphate) represents an important innovation for improving nitrogen and phosphorus nutrition in crops. Developed by the Indian Farmers Fertiliser Cooperative Limited, Nano DAP contains nitrogen and phosphorus nanoparticles designed for rapid absorption and efficient utilization by plants. Unlike conventional DAP fertilizer, which often suffers from phosphorus fixation in soil and low nutrient use

efficiency, Nano DAP provides nutrients in nano-sized particles that are readily available to plants. This technology has the potential to reduce the dependence on bulk chemical fertilizers while maintaining crop productivity and improving fertilizer use efficiency (IFFCO, 2023). Phosphorus plays a critical role during seed germination and early seedling development. It is involved in energy transfer through ATP synthesis, nucleic acid formation, cell division, root initiation, and enzyme activation. Adequate phosphorus availability during the initial growth stages enhances root proliferation, promotes vigorous seedling growth, and enables plants to establish more rapidly under field conditions. Nitrogen, another major constituent of Nano DAP, is equally important for chlorophyll synthesis, protein formation, and vegetative growth. Therefore, treating wheat seeds with Nano DAP before sowing may improve nutrient availability immediately after germination, resulting in better crop establishment and enhanced early plant growth. Recent studies have demonstrated that nanofertilizers improve seed germination, seedling vigour, nutrient uptake, photosynthetic efficiency, and crop productivity across several agricultural crops. Their use also contributes to sustainable agriculture by reducing fertilizer application rates, improving nutrient recovery efficiency, and lowering environmental contamination. Nevertheless, field-based information regarding the use of Nano DAP as a seed treatment in wheat under the agro-climatic conditions of southeastern Rajasthan remains limited. Scientific evaluation under local conditions is therefore essential before recommending this technology for large-scale adoption. Keeping these aspects in view, a field experiment was conducted during the Rabi season of 2025–26 at the Agricultural Instructional Farm, School of Agricultural Sciences, Career Point University, Kota, Rajasthan. The experiment aimed to evaluate the effect of Nano DAP used as a seed treatment on wheat seed germination, seedling emergence, early crop establishment, and initial vegetative growth. The study also sought to assess the practical feasibility of Nano DAP seed treatment as a sustainable nutrient management strategy that could improve fertilizer use efficiency while reducing dependence on conventional phosphorus fertilizers. The findings of this study are expected to contribute valuable information regarding the application of nanotechnology in wheat production and provide scientific evidence for the promotion of Nano DAP as an innovative input for sustainable cereal cultivation.

2. Materials and Methods:

The present investigation entitled "Effect of Nano DAP Seed Treatment on Germination and Early Growth of Wheat (*Triticum aestivum* L.)" was conducted during the Rabi season of 2025–26 at the Agricultural Instructional Farm, School of Agricultural Sciences, Career Point University, Kota, Rajasthan, India. The study was undertaken to evaluate the effect of Nano DAP seed treatment on seed germination, seedling vigour, and early growth of wheat under field conditions. The experiment aimed to assess the potential of Nano DAP as an innovative nanofertilizer for improving early crop establishment, enhancing nutrient use efficiency, and promoting sustainable wheat production. The wheat variety Raj-4037 was selected for the study owing to its adaptability and widespread cultivation in the region. Healthy, bold, and uniformly sized seeds with high physical purity were used to eliminate variability arising from seed quality. The seeds were divided into two experimental groups: **T₁**: Untreated seeds (Control) , **T₂**: Seeds treated with Nano DAP Nano DAP was applied at the recommended rate of 5 ml kg⁻¹ of seed. The required quantity of Nano DAP was measured accurately and mixed thoroughly with the seeds in a clean plastic container to ensure a uniform coating on the entire seed surface. The treated seeds were gently mixed until all seeds received an even layer of the Nano DAP formulation. After treatment, the seeds were spread in a thin layer and allowed to dry under shade for approximately 30–60 minutes, avoiding direct sunlight to maintain the stability and effectiveness of the nano-formulation. The untreated seeds were kept separately and handled in the same manner without Nano DAP application. Both treated and untreated seeds were sown on the same day under identical field conditions to eliminate environmental variation. The experiment was maintained under uniform agronomic practices with respect to land preparation, sowing depth, irrigation, and crop management so that any observed differences could be attributed primarily to the Nano DAP seed treatment. Care was taken to maintain similar soil moisture, temperature, and field conditions throughout the germination and early crop establishment period. To evaluate the influence of Nano DAP on seed performance and early crop growth, observations were recorded at regular intervals after sowing. The following parameters were assessed. The recorded data from Nano DAP-treated and untreated (control) seeds were compared to determine the effect of Nano DAP on germination behaviour, seedling vigour, and early crop establishment. Descriptive statistical analysis and graphical comparisons were used to interpret the experimental results.



T₁: Untreated seeds (Control)



T₂: Seeds treated with Nano DAP

3. Review of Literature

The application of nanotechnology in agriculture has opened new opportunities for improving fertilizer use efficiency, enhancing crop productivity, and promoting sustainable farming systems. Among various nanofertilizers, Nano Di-Ammonium Phosphate (Nano DAP) has recently gained attention as an efficient source of nitrogen and phosphorus for crop production. Several researchers have reported positive effects of nanofertilizers on seed germination, nutrient uptake, seedling vigour, crop growth, and yield. Copeland and McDonald (2001) reported that seed treatment is one of the most effective methods for improving seed germination, protecting seeds from biotic stresses, and promoting vigorous seedling establishment. Healthy and vigorous seedlings establish better under field conditions and ultimately contribute to higher crop productivity. Subramanian *et al.* (2015) described nanofertilizers as advanced nutrient delivery systems capable of supplying nutrients in a controlled and efficient manner. According to the authors, nanofertilizers increase nutrient availability, reduce nutrient losses, and improve fertilizer use efficiency compared with conventional fertilizers. Dimkpa and Bindraban (2018) reviewed the potential of nanofertilizers in modern agriculture and reported that nano-based nutrient formulations improve nutrient absorption, stimulate plant growth, enhance root development, and increase crop productivity while minimizing environmental pollution caused by excessive fertilizer

use. Kah *et al.* (2018) explained that nanoparticles possess a high surface area and greater reactivity, allowing nutrients to be released gradually and absorbed more efficiently by plants. Their review concluded that nanofertilizers have considerable potential to improve nutrient use efficiency and support sustainable agricultural production. Taiz *et al.* (2018) emphasized the importance of nitrogen and phosphorus during seed germination and early plant growth. Phosphorus plays a key role in ATP synthesis, energy transfer, root initiation, and cell division, whereas nitrogen is essential for chlorophyll formation, protein synthesis, and vegetative growth. Adequate availability of these nutrients during the early stages promotes vigorous seedling development. Indian Farmers Fertiliser Cooperative Limited (2023) introduced Nano DAP as a next-generation phosphorus fertilizer containing nano-sized particles of nitrogen and phosphorus. According to the technical bulletin, Nano DAP improves nutrient availability, enhances fertilizer use efficiency, reduces phosphorus fixation in soil, and can partially substitute conventional DAP fertilizer. Food and Agriculture Organization of the United Nations (2023) emphasized that improving nutrient use efficiency is essential for ensuring future food security while reducing the environmental impacts associated with excessive fertilizer application. The organization recommended innovative fertilizer technologies for sustainable crop production. Indian Council of Agricultural Research (2024) highlighted the importance of balanced nutrient management and advanced fertilizer technologies for increasing wheat productivity in India. The report indicated that improving nutrient use efficiency is necessary to sustain crop production under changing climatic conditions. Recent experimental studies conducted on cereal and pulse crops have also demonstrated that nanofertilizers improve seed germination, seedling vigour, chlorophyll content, nutrient uptake, root growth, and overall crop performance. These improvements are primarily attributed to the enhanced availability and efficient utilization of nutrients supplied through nano-sized particles. Although several studies have reported the beneficial effects of nanofertilizers, information regarding the use of Nano DAP as a seed treatment in wheat under the agro-climatic conditions of southeastern Rajasthan remains limited. Therefore, the present investigation was undertaken to evaluate the effect of Nano DAP seed treatment on germination, seedling vigour, and early crop establishment of wheat under field conditions.

4. Results and Discussion

The application of Nano DAP as a seed treatment had a positive influence on the germination behaviour and early seedling development of wheat (*Triticum aestivum* L.) under field conditions. The comparative evaluation between Nano DAP-treated seeds and untreated (control) seeds revealed noticeable improvements in several growth parameters during the initial stages of crop establishment. The Nano DAP-treated seeds initiated germination earlier than the untreated seeds, indicating that the nano-formulation facilitated quicker metabolic activation during the germination process. Early germination is considered an important agronomic advantage because it promotes rapid crop establishment, enhances competitiveness against weeds, and enables better utilization of available soil moisture and nutrients (Copeland and McDonald, 2001). A comparatively higher germination percentage was recorded in the Nano DAP-treated seeds than in the untreated control. The improved germination may be attributed to the enhanced availability of nitrogen and phosphorus supplied through nano-sized particles, which are readily absorbed by the germinating embryo. Phosphorus is an essential component of ATP, nucleic acids, and phospholipids, playing a vital role in energy transfer, cell division, and root initiation during seed germination. Likewise, nitrogen supports the synthesis of amino acids, proteins, chlorophyll, and enzymes required for early seedling growth (Taiz *et al.*, 2018). Besides increasing germination percentage, Nano DAP treatment also improved the uniformity of seedling emergence. The treated plots exhibited a more homogeneous crop stand, with seedlings emerging almost simultaneously, whereas the control plots showed comparatively irregular and uneven emergence. Uniform crop establishment is highly desirable because it facilitates efficient crop management practices, reduces inter-plant competition, and ultimately contributes to higher productivity. The beneficial effect of Nano DAP was further reflected in the early vegetative growth of wheat seedlings. Seedlings originating from treated seeds appeared more vigorous, healthier, and greener than those in the control treatment. Visual observations indicated improved shoot growth, enhanced leaf development, and better overall plant appearance during the early growth stages. One of the most noticeable observations was the superior root development in Nano DAP-treated plants. The seedlings produced comparatively stronger and more active root systems, which are essential for efficient absorption of water and nutrients from the soil. Enhanced root growth during the initial stages generally improves crop resilience under moisture stress and supports better vegetative

development throughout the growing season. Similar observations have been reported in previous studies, where nanofertilizers promoted root elongation, nutrient uptake, and seedling vigour by increasing nutrient availability and improving fertilizer use efficiency (Dimkpa and Bindraban, 2018; Kah *et al.*, 2018). The untreated control plants, although germinating satisfactorily, exhibited comparatively lower germination percentage, delayed emergence, and less uniform crop establishment. Seedlings were relatively smaller during the early stages and displayed comparatively weaker root development than those produced from Nano DAP-treated seeds. An important finding of the present investigation was that only 5 ml of Nano DAP per kilogram of seed was sufficient to produce visible improvements in seed performance and early crop growth. This demonstrates the high nutrient use efficiency of nano-fertilizers, as very small quantities can provide significant physiological benefits. Unlike conventional phosphorus fertilizers, which often undergo fixation in soil and become unavailable to plants, Nano DAP supplies nutrients in nano-sized particles that improve nutrient absorption and utilization by emerging seedlings (IFFCO, 2023). Overall, the experimental observations suggest that Nano DAP seed treatment enhanced germination percentage, accelerated seedling emergence, improved crop stand uniformity, promoted vigorous root and shoot growth, and strengthened early crop establishment. These improvements indicate that Nano DAP has considerable potential as a sustainable seed treatment technology for wheat cultivation, contributing to improved nutrient use efficiency while reducing dependence on large quantities of conventional phosphorus fertilizers. Nanotechnology-based fertilizers have emerged as one of the most promising innovations in modern agriculture due to their ability to improve nutrient use efficiency, enhance crop productivity, and support sustainable farming systems. Unlike conventional fertilizers, which often suffer substantial nutrient losses through leaching, volatilization, runoff, and soil fixation, nanofertilizers are designed to deliver nutrients in nano-sized particles that possess a larger surface area, greater reactivity, and improved penetration into plant tissues. Consequently, nutrients become available to plants more efficiently and in a controlled manner, resulting in enhanced nutrient uptake and utilization (Dimkpa & Bindraban, 2018; Kah *et al.*, 2018). The findings of the present study indicate that Nano DAP seed treatment positively influenced wheat germination, seedling vigour, and early crop establishment. The enhanced germination percentage and uniform seedling emergence observed in the treated seeds suggest that Nano DAP supplied readily available nitrogen and phosphorus during the critical stages of germination and early growth. Phosphorus is indispensable for ATP

production, nucleic acid synthesis, root initiation, and cell division, whereas nitrogen plays a central role in protein synthesis, chlorophyll formation, and enzymatic activity. Adequate availability of these nutrients immediately after germination enables seedlings to establish rapidly and develop vigorous root and shoot systems (Taiz *et al.*, 2018). Improved seedling establishment is particularly important because the initial growth stage determines the future growth potential of the crop. A vigorous crop stand ensures better utilization of sunlight, water, and nutrients, enhances competition against weeds, and improves the plant's ability to withstand biotic and abiotic stresses. Therefore, the positive effects of Nano DAP observed during the early stages may ultimately contribute to higher biomass production, improved yield attributes, and better grain productivity under field conditions, although these parameters require further validation through full-season experiments. One of the most significant observations of this investigation was that only 5 ml of Nano DAP per kilogram of seed produced noticeable improvements in germination and early plant growth. This demonstrates the high efficiency of nanofertilizers, where very small quantities are capable of producing measurable physiological responses. Such enhanced efficiency is primarily attributed to the nano-scale size of fertilizer particles, which increases nutrient availability while reducing nutrient losses caused by soil fixation, especially in the case of phosphorus. Conventional phosphorus fertilizers frequently become unavailable to plants due to fixation with calcium, iron, and aluminum compounds in soil, whereas nano-formulations are designed to improve nutrient accessibility and utilization (IFFCO, 2023). From the perspective of sustainable agriculture, Nano DAP offers several practical advantages. Improved nutrient use efficiency may reduce the requirement for conventional chemical fertilizers, thereby lowering input costs for farmers. Reduced fertilizer application can also decrease nutrient losses into the environment, minimizing groundwater contamination, eutrophication of water bodies, and greenhouse gas emissions associated with fertilizer manufacture and application. Consequently, nanofertilizers have the potential to contribute significantly to environmentally sustainable and climate-smart agricultural production systems (Kah *et al.*, 2018). The present study further supports the concept that seed treatment represents an efficient method of nutrient delivery, as nutrients become available precisely when seedlings require them most. Providing essential nutrients at the time of sowing allows plants to establish a stronger root system and healthier canopy from the beginning of the crop cycle. Such early advantages frequently translate into improved crop performance throughout subsequent growth stages. Nevertheless, despite the encouraging results, the present

investigation was confined primarily to observations on germination and early seedling

Treatment	Germination initiation (DAS)	Germination (%)	Seedling emergence (%)	Plant height at 15 DAS (cm)	Root length at 15 DAS (cm)	Shoot length at 15 DAS (cm)	Seedling vigour	Crop stand uniformity
T1: Untreated wheat seeds (Control)	5	86	84	14.2	8.3	10.6	Moderate	Moderate
T2: Wheat seeds treated with Nano DAP @ 5 ml kg ⁻¹ seed	4	95	94	17.1	10.8	12.9	High	Excellent

growth under a single environmental condition and one wheat variety. Therefore, additional research is required to validate these findings across different agro-climatic regions, soil types, wheat cultivars, and management practices. Future investigations should also evaluate the influence of Nano DAP on nutrient uptake, physiological characteristics, photosynthetic efficiency, yield components, grain quality, fertilizer use efficiency, economic returns, and long-term soil health. Multi-location field trials conducted over several cropping seasons will provide stronger scientific evidence regarding the consistency and practical applicability of Nano DAP technology under diverse farming conditions.

5. Conclusion:

The present investigation demonstrated that Nano DAP seed treatment at 5 ml kg⁻¹ seed significantly improved the germination and early growth of wheat compared with untreated seeds. Nano DAP-treated seeds showed earlier and higher germination, better seedling emergence, stronger root and shoot development, and more uniform crop establishment. These improvements indicate enhanced nutrient availability during the critical stages of seed germination and early seedling growth, resulting in better seedling vigour and crop establishment. The study further revealed that a very small quantity of Nano DAP was sufficient to produce noticeable improvements in early crop performance, highlighting its high nutrient use efficiency. Nano DAP therefore represents a promising nanofertilizer technology that can contribute to sustainable wheat production by improving fertilizer efficiency while reducing dependence on conventional phosphorus fertilizers. Although the

results are encouraging, the study was limited to the early growth stage under a single location and one wheat variety. Further research involving different agro-climatic conditions, wheat cultivars, and complete crop growth cycles is needed to confirm its effects on nutrient uptake, grain yield, grain quality, economic returns, and long-term soil health. Nevertheless, the present findings suggest that Nano DAP seed treatment can be recommended as an effective strategy for improving early crop establishment and supporting sustainable nutrient management in wheat cultivation.

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Effect of Nitrogen- and Phosphorus-Based Liquid Biofertilizers on Growth and Yield Attributes of Chickpea (*Cicer arietinum* L.)

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Abstract

Chickpea (*Cicer arietinum* L.) is one of the most important pulse crops cultivated in India due to its high nutritional value, ability to fix atmospheric nitrogen, and adaptability to diverse agro-climatic conditions. However, declining soil fertility, low phosphorus availability, and excessive dependence on chemical fertilizers have emerged as major constraints to sustainable chickpea production. Liquid bio-fertilizers containing beneficial microorganisms such as Rhizobium and phosphorus-solubilizing bacteria (PSB) offer an eco-friendly and cost-effective alternative for enhancing nutrient availability, improving soil health, and increasing crop productivity. Keeping these aspects in view, a field experiment entitled “Influence of Nitrogen- and Phosphorus-Based Liquid Biofertilizers on Growth, Yield, and Nutrient Uptake of Chickpea (*Cicer arietinum* L.)” was conducted during the rabi season of 2022–23 at the Department of Agronomy, School of Agricultural Sciences, Career Point University, Kota, Rajasthan, India. The experiment was laid out in a Factorial Randomized Block Design (FRBD) with three replications, comprising sixteen treatment combinations involving four fertility levels [control (F_0), 10 kg N + 30 kg P_2O_5 ha⁻¹ (F_1), 15 kg N + 40 kg P_2O_5 ha⁻¹ (F_2), and 20 kg N + 50 kg P_2O_5 ha⁻¹ (F_3)] and four liquid biofertilizer treatments [control (LB_0), liquid Rhizobium inoculation (LB_1), liquid PSB inoculation (LB_2), and combined liquid Rhizobium + PSB inoculation (LB_3)]. Chickpea variety GNG-1958 was sown at a spacing of 30 × 10 cm using a seed rate of 80 kg ha⁻¹. Growth parameters, nodulation, yield attributes, seed and haulm yield, nutrient uptake, protein content, chlorophyll content, soil fertility status, and economic returns were recorded and analyzed. The experimental soil was clay loam in texture, slightly alkaline in reaction (pH 8.03), low in available nitrogen, medium in available phosphorus, and high in available potassium. The study aimed to evaluate the influence of integrated nutrient management through nitrogen,

phosphorus, and liquid bio-fertilizers on crop growth, productivity, nutrient uptake, and profitability. It was hypothesized that the combined application of recommended nitrogen and phosphorus levels with liquid Rhizobium and PSB inoculation would enhance nodulation, nutrient availability, physiological efficiency, and yield while improving soil fertility and reducing dependence on chemical fertilizers. The investigation provides valuable insights into sustainable nutrient management strategies for chickpea cultivation under the humid south-eastern plain region of Rajasthan. The findings are expected to support the development of economically viable and environmentally sustainable fertilizer recommendations by integrating inorganic fertilizers with liquid bio-fertilizers, thereby contributing to improved productivity, soil health, and long-term agricultural sustainability.

Keywords: Nitrogen, Phosphorus, Bio-fertilizers, Chickpea.

1. Introduction

Chickpea (*Cicer arietinum* L.) is an important cool-season food legume belonging to the family Leguminaceae and subfamily Papilionaceae. It is one of the most widely cultivated pulse crops worldwide and plays a pivotal role in ensuring food and nutritional security, particularly in developing countries. In India, chickpea occupies the largest share among pulse crops, covering approximately 9.44 million hectares with a production of 10.13 million tonnes and an average productivity of 1,073 kg ha⁻¹. More than 90% of the country's chickpea production is concentrated in the major growing states of Madhya Pradesh, Rajasthan, Maharashtra, Uttar Pradesh, Karnataka, Chhattisgarh, Andhra Pradesh, Gujarat, Jharkhand, Tamil Nadu, and Telangana. Rajasthan is one of the leading chickpea-producing states, where the crop is cultivated over an area of 1.60 million hectares, producing 1.76 million tonnes with an average productivity of 1,103 kg ha⁻¹ (Government of India, 2018–19). Chickpea possesses a well-developed and deep taproot system, enabling it to withstand drought and moisture-deficit conditions more effectively than many other pulse crops. This characteristic makes it highly suitable for cultivation under both rainfed and limited-irrigation farming systems. The crop is predominantly grown under tropical and subtropical climatic conditions, where it serves as an important component of sustainable cropping systems due to its adaptability, nitrogen-fixing ability, and relatively low input requirements. Owing to its wide adaptability, economic significance, and substantial contribution to pulse production, chickpea is popularly regarded as the "King of Pulses. Chickpea is cultivated primarily for its

exceptional nutritional value and is considered one of the most important sources of plant-based protein in human diets. Pulse grains generally contain 20–25% protein, which is nearly twice that of wheat and about three times higher than that of rice, making them an indispensable component of balanced nutrition, particularly in vegetarian populations (Pingoliya *et al.*, 2013). Besides being an excellent source of high-quality protein, chickpea provides essential amino acids, complex carbohydrates, dietary fiber, vitamins, and minerals that contribute significantly to human health. Regular consumption of pulses has been associated with a reduced risk of several non-communicable diseases, including cardiovascular disorders, obesity, diabetes, and certain types of cancer owing to their low glycaemic index and high antioxidant content (Jukanti *et al.*, 2012). Nutritionally, chickpea seeds contain approximately 20% protein, 52–70% carbohydrates, 4–10% fat, 6% crude fibre, 49–53 mg phosphorus, and 7 mg iron per 100 g of edible portion (Deppe, 2010). They are also rich in vitamins such as thiamine, riboflavin, niacin, biotin, vitamin A, and vitamin C, making them a valuable source of essential micronutrients. Chickpea is consumed in diverse forms, including whole boiled or roasted seeds, sprouted grains, split dal, flour (besan), and various processed food products. In addition to its nutritional importance, chickpea possesses several medicinal properties. Germinated seeds are considered beneficial for preventing vitamin C deficiency-related disorders, while regular consumption has been reported to support blood purification and overall metabolic health. Nitrogen (N) is one of the most essential macronutrients required for optimum plant growth and development. It is a fundamental constituent of amino acids, proteins, nucleic acids, chlorophyll, phospholipids, enzymes, vitamins, and several plant hormones, thereby playing a central role in numerous physiological and biochemical processes. In leguminous crops such as chickpea, atmospheric nitrogen is biologically fixed through a symbiotic association with *Rhizobium* bacteria present in root nodules, reducing dependence on synthetic nitrogen fertilizers. However, a small starter dose of nitrogen at sowing is often recommended to promote early seedling establishment, vigorous vegetative growth, rapid leaf area development, and enhanced photosynthetic efficiency before effective nodulation occurs. Consequently, adequate nitrogen availability during the initial stages of crop growth contributes significantly to improved biomass production, better reproductive development, and higher seed yield. Phosphorus (P) is an essential macronutrient that plays a fundamental role in plant growth, metabolism, and productivity. It is actively involved in several physiological and biochemical processes, including photosynthesis, energy transfer, carbohydrate metabolism, and the

synthesis of nucleic acids and cellular membranes. Phosphorus is a key constituent of high-energy compounds such as adenosine triphosphate (ATP) and adenosine diphosphate (ADP), as well as phospholipids, phytin, nucleic acids, and nicotinamide adenine dinucleotide phosphate (NADP), all of which are indispensable for normal plant development. Adequate phosphorus nutrition promotes vigorous root growth, enhances root length and biomass, stimulates rhizobial activity and nodule formation, and improves flowering, pod development, seed filling, and test weight, ultimately resulting in increased grain yield (Shahzad *et al.*, 2014). Biofertilizers have emerged as an eco-friendly and sustainable alternative to chemical fertilizers by enhancing nutrient availability through the activity of beneficial microorganisms. These microbial inoculants contain viable strains of nitrogen-fixing bacteria, phosphorus-solubilizing bacteria (PSB), and other plant growth-promoting microorganisms capable of mobilizing essential nutrients into forms readily available for plant uptake. Their application not only improves nutrient use efficiency but also enhances soil biological activity, promotes root growth, and contributes to the maintenance of soil health. In leguminous crops such as chickpea, symbiotic nitrogen-fixing bacteria (*Rhizobium*) establish associations with root nodules to fix atmospheric nitrogen, while phosphorus-solubilizing bacteria convert insoluble soil phosphorus into plant-available forms. The combined use of *Rhizobium* and PSB has been reported to improve nodulation, nutrient uptake, plant growth, grain yield, and overall crop productivity while reducing dependence on synthetic fertilizers, thereby supporting sustainable agricultural production systems (Selvakumar *et al.*, 2012).

Liquid bio-fertilizers represent an advanced formulation of microbial inoculants that contain highly efficient strains of beneficial microorganisms suspended in a nutrient-rich liquid medium along with suitable protectants and additives that enhance microbial survival during storage and after application to seeds or soil. These additives improve inoculant quality by maintaining high microbial viability, increasing cell population density, and extending shelf life (Tittabutre *et al.*, 2007). Compared with conventional carrier-based formulations, liquid bio-fertilizers offer several advantages, including a longer shelf life of one year or more, higher microbial survival, reduced contamination, and improved field performance. In contrast, carrier-based bio-fertilizers generally have a shelf life of less than six months and are often affected by low water activity, poor survival of inoculated microorganisms, and contamination during storage.

2. Materials and Methods:

A field experiment entitled “Effect of Nitrogen- and Phosphorus-Based Liquid Biofertilizers on Growth and Yield Attributes of Chickpea (*Cicer arietinum* L.)” was conducted during the rabi season of 2025–26 at the Agricultural Instructional Farm, School of Agricultural Sciences, Career Point University, Kota, Rajasthan, India. The study was undertaken to investigate the influence of varying nitrogen and phosphorus fertility levels in combination with liquid biofertilizer inoculation on the growth, yield attributes, productivity, nutrient uptake, and economic performance of chickpea. The experimental farm is situated in the Humid South-Eastern Plain Agro-climatic Zone (Zone V) of Rajasthan, encompassing approximately 2.443 million hectares, which accounts for nearly 7.71% of the state's total geographical area. Geographically, the region extends between 23°45' and 26°33' N latitude and 75°27' and 77°26' E longitude. The research farm is equipped with modern infrastructure and essential facilities, including irrigation systems, laboratory facilities, and analytical instruments required for conducting agronomic field experiments. The study area experiences a subtropical climate, characterized by mild winters, moderately warm summers, and relatively high humidity during the southwest monsoon season. The average annual rainfall ranges from 800 to 1000 mm, with approximately 85–90% of the total precipitation received between July and September under the influence of the southwest monsoon. During the rabi season of 2025–26, the maximum air temperature ranged from 21.0 to 30.2°C, while the minimum temperature varied between 4.4 and 17.5°C. The experimental site received a total rainfall of 15.40 mm during the crop-growing period. Overall, the prevailing weather conditions were favourable for the successful establishment, growth, and development of the chickpea crop. Prior to the commencement of the experiment, representative soil samples were collected randomly from the experimental field at a depth of 0–15 cm to assess the initial physico-chemical properties of the soil. The individual samples were thoroughly mixed to obtain a composite sample, which was subsequently air-dried, ground, and passed through a 2-mm sieve for laboratory analysis. The experimental soil was clay loam in texture, containing 37.58% sand, 25.86% silt, and 35.40% clay. The physical properties of the soil included a bulk density of 1.45 Mg m⁻³, particle density of 2.51 Mg m⁻³, and porosity of 43.50%. The soil was slightly alkaline in reaction with a pH of 8.03 and an electrical conductivity (EC) of 0.63 dS m⁻¹, indicating non-saline conditions. The soil contained 0.643% organic carbon, 276.25 kg available nitrogen ha⁻¹, 18.62 kg available phosphorus

ha⁻¹, and 360.70 kg available potassium ha⁻¹, representing low available nitrogen, medium available phosphorus, and high available potassium status.

3. Review of Literature

Khoja *et al.* (2002) conducted a field experiment at Jobner (Rajasthan) and revealed that 20 kg N ha⁻¹ + 20 kg P₂O₅ kg ha⁻¹ significantly increased the plant height over control and 10 kg N ha⁻¹ + 20 kg P₂O₅ ha⁻¹. The number of branches plant⁻¹ and dry matter accumulation plant⁻¹ were increased due to 10 kg N + 20 kg P₂O₅ ha⁻¹ over control in chickpea. Tiwari *et al.* (2005) revealed that application of phosphorus at 50 kg P₂O₅ ha⁻¹ significantly increased the number of pods plant⁻¹, test weight, seed and haulm yield and harvest index over control and 25 kg P₂O₅ ha⁻¹ in chickpea. Dotaniya *et al.* (2014) revealed that seed yield of chickpea significantly increased with increasing level of phosphorus and maximum was at 60 kg P₂O₅ ha⁻¹. Kumar *et al.* (2014) resulted that 100 per cent RDF recorded significantly highest number of pods plant⁻¹ (44.19), seed yield (1854 kg ha⁻¹) and haulm yield (2722 kg ha⁻¹) over 75 per cent RDF and 50 per cent RDF in chickpea. Badini *et al.* (2015) revealed that 55 kg P₂O₅ ha⁻¹ higher yield attributes viz., high number of pods plant⁻¹, seeds plant⁻¹, seed index and seed yield (1564.15 kg ha⁻¹) over other levels in chickpea. Jat and Ahlawat (2004) revealed that application of phosphorus up to 26.4 kg P₂O₅ ha⁻¹ significantly increased the total uptake of nitrogen and phosphorus over control in chickpea. Meena *et al.* (2001) revealed that the protein content in seed was significantly higher with application of 60 kg P₂O₅ ha⁻¹ over control in chickpea. Khoja *et al.* (2002) revealed that seed treated with *Rhizobium* + PSB significantly increased the plant height, number of branches plant⁻¹ and dry matter accumulation plant⁻¹ over control in chickpea. Jat and Ahlawat (2004) revealed that seed inoculation with *Rhizobium* and PSB enhanced seed yield (2.40 ton ha⁻¹) and haulm yield (3.80 ton ha⁻¹) in chickpea.

4. Results and Discussion

The present field experiment entitled “Effect of Nitrogen- and Phosphorus-Based Liquid Biofertilizers on Growth and Yield Attributes of Chickpea (*Cicer arietinum* L.)” was conducted during the rabi season of 2025–26 at the School of Agricultural Sciences, Career Point University, Kota, Rajasthan. The experimental data were statistically analyzed, and the

significant effects of treatments are presented in the form of tables and graphs, while the analysis of variance (ANOVA) is provided in the appendices. Plant population recorded at 15 DAS and at harvest remained statistically unaffected by different fertility levels as well as liquid bio-fertilizer treatments. Plant height at 30 DAS also did not differ significantly among treatments, although the highest value of 19.89 cm was observed under F_3 (20 kg N + 50 kg P_2O_5 ha⁻¹). However, at 60 DAS, plant height increased significantly with increasing fertility levels, with the tallest plants (43.56 cm) recorded under F_3 and the shortest (37.02 cm) under the control treatment. Similarly, co-inoculation with Liquid Rhizobium + Liquid PSB (LB_3) resulted in the maximum plant height (41.46 cm), significantly outperforming the uninoculated control. At harvest, the highest plant height was recorded under F_3 (54.85 cm) and LB_3 (53.50 cm), indicating that balanced fertilization and bio-fertilizer co-inoculation promoted vigorous crop growth. The number of branches per plant also increased significantly with increasing fertility levels and liquid bio-fertilizer application throughout the crop growth period. At 30 DAS, the highest number of branches was recorded under F_3 (4.33) and LB_3 (4.16). At 60 DAS, F_3 produced 9.51 branches plant⁻¹, while LB_3 recorded 8.84 branches plant⁻¹, both significantly higher than the control. At harvest, the maximum number of branches was observed under F_3 (12.24 branches plant⁻¹) and LB_3 (12.09 branches plant⁻¹), confirming that the combined application of nitrogen, phosphorus, and Liquid Rhizobium + Liquid PSB enhanced the vegetative growth of chickpea. Application of increasing fertility levels significantly improved growth characters such as plant height, number of branches, dry matter accumulation, and nodulation, with the highest values recorded under F_3 (20 kg N + 50 kg P_2O_5 ha⁻¹). In contrast, plant population, plant height at 30 DAS, and days to 50% flowering were not significantly influenced by fertility treatments. The enhanced growth under higher fertility levels may be attributed to the role of nitrogen in chlorophyll synthesis and vegetative development, together with the beneficial effects of phosphorus on root development, nodulation, ATP synthesis, nutrient uptake, and energy transfer, supporting earlier findings reported by Khoja *et al.* (2002) and Islam *et al.* (2013). The highest fertility level also significantly increased pods per plant, seeds per pod, seed weight per plant, and consequently seed yield, haulm yield, and biological yield. Improved nutrient availability promoted better source-sink relationships, resulting in enhanced crop productivity. Seed yield showed a strong positive association with branches, dry matter accumulation, pods per plant, seeds per pod, and seed weight, which corroborates the findings of Ali *et al.* (2010). Although nitrogen and phosphorus concentrations in seed and haulm were not significantly

affected, F_3 significantly enhanced nutrient uptake, soil available nitrogen and phosphorus, chlorophyll content, and seed protein content, thereby improving crop quality and productivity. These results are in accordance with the findings of Singh and Prasad (2008). Economically, the highest net return (₹70,553 ha^{-1}) and benefit–cost ratio (2.32) were obtained with F_3 (20 kg N + 50 kg P_2O_5 ha^{-1}) due to its superior seed yield, which agrees with the observations of Ali *et al.* (2010).

The application of liquid bio-fertilizers also exerted a significant influence on crop performance. Co-inoculation of Liquid Rhizobium + Liquid PSB (LB_3) significantly improved plant height, number of branches, dry matter accumulation, and nodulation compared with the control treatment. These improvements can be attributed to enhanced biological nitrogen fixation, phosphorus solubilization, increased nutrient availability, and the production of plant growth-promoting substances, as also reported by Togay *et al.* (2008). Among the bio-fertilizer treatments, LB_3 recorded the highest number of pods per plant, seed weight per plant, seed yield, biological yield, and harvest index. The improved nutrient availability and synthesis of plant growth regulators enhanced both yield attributes and overall productivity, while seed yield remained positively associated with major growth and yield components, confirming the findings of Sahai and Chandra (2011). Co-inoculation with Rhizobium and PSB significantly increased nitrogen and phosphorus uptake, soil nutrient availability, chlorophyll content, and seed protein content, although nutrient concentrations in seed and haulm remained statistically unchanged. Similar observations were reported by Gupta and Gangwar (2012). From an economic perspective, LB_3 (Liquid Rhizobium + Liquid PSB) produced the highest net return (₹68,457 ha^{-1}) and benefit–cost ratio (2.32) owing to higher yield and improved nutrient use efficiency. The interaction between fertility levels and liquid bio-fertilizer treatments significantly influenced dry matter accumulation, nodulation, pods per plant, and seed weight per plant. The combined application of F_3 (20 kg N + 50 kg P_2O_5 ha^{-1}) with LB_3 (Liquid Rhizobium + Liquid PSB) produced the highest values for these parameters, resulting in superior crop growth, enhanced nutrient availability, increased nitrogen fixation and phosphorus solubilization, improved source–sink relationships, and ultimately higher productivity. These findings are in close agreement with those reported by Kumar *et al.* (2014).

Table 1.1: Effect of fertility levels and liquid bio-fertilizers inoculation on yield attributes and yield of chickpea

Treatments	Num ber of pods plant ⁻¹	Num ber of seeds pod ⁻¹	Weig ht of seeds plant ⁻¹ (g)	Seed inde x (100 seeds weig ht)	Yield (kg ha ⁻¹)			HI (%)
					Se ed	Haul m	Biologi cal	
Fertility levels								
Control	55.17	2.15	23.98	20.00	1490	2264	3754	39.62
10 kg N + 30 kg P ₂ O ₅ ha ⁻¹	74.26	2.16	34.99	20.13	1713	2409	4129	41.50
15 kg N + 40 kg P ₂ O ₅ ha ⁻¹	85.08	2.30	36.34	21.22	1790	2431	4222	42.38
20 kg N + 50 kg P ₂ O ₅ ha ⁻¹	91.25	2.51	39.65	21.16	1912	2577	4489	42.58
SEm±	1.03	0.08	1.07	0.43	26	32	35	0.58
CD (P= 0.05)	2.97	0.22	3.10	NS	76	94	102	1.69
Liquid bio-fertilizers								
Control	57.67	1.95	26.90	19.95	1550	2375	3925	39.42
Liquid <i>Rhizobium</i> inoculation alone	80.92	2.42	34.41	20.72	1781	2441	4221	42.11
Liquid PSB inoculation alone	76.08	2.32	33.37	20.65	1718	2413	4130	41.51
Liquid <i>Rhizobium</i> + liquid PSB inoculation	91.08	2.43	40.28	21.20	1856	2454	4310	43.03
SEm±	1.03	0.08	1.07	0.43	26	32	35	0.58
CD (P= 0.05)	2.97	0.22	3.10	NS	76	NS	102	1.69

5. Conclusion:

The present study demonstrated that integrated application of 20 kg N + 50 kg P₂O₅ ha⁻¹ (F₃) along with Liquid Rhizobium + Liquid PSB (LB₃) significantly improved the growth, yield attributes, seed yield, nutrient uptake, chlorophyll content, seed protein content, and economic returns of chickpea under the agro-climatic conditions of South-Eastern Rajasthan. The combined application of balanced nitrogen and phosphorus fertilization with liquid bio-fertilizer inoculation enhanced nutrient availability, biological nitrogen fixation, phosphorus solubilization, and overall crop productivity. Therefore, the use of 20 kg N + 50 kg P₂O₅ ha⁻¹ along with Liquid Rhizobium + Liquid PSB is recommended as an efficient, economical, and sustainable nutrient management practice for chickpea cultivation.

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